

# A Model of Electric Field Assisted Capillarity for the Fabrication of Hollow Microstructures

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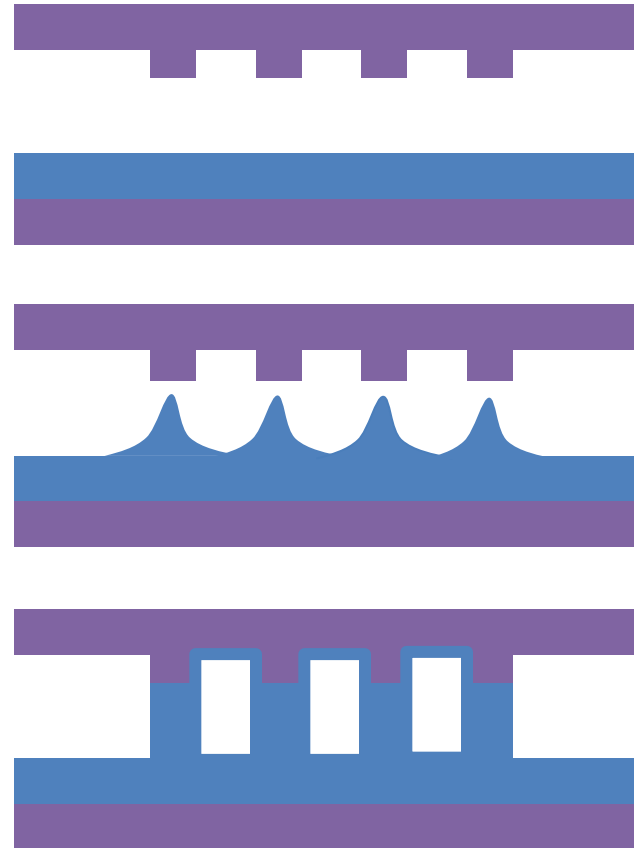
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# What is Electric Field Assisted Capillarity (EFAC)?

- A process which patterns polymers using electric fields
- Polymers must be semi-molten
- Initially surface driven by electric field
- When the polymer reaches the top mask Capillary force becomes dominant
- This causes the polymer to coat the top mask forming a hollow microstructure



# Forces

## Electrostatic and Dielectric Forces

- These are the dominant force at the start of the process
- They are concentrated around the polymer/air interface
- It is proportional to the square of the electric field

## Capillary Force

- This becomes dominant when the polymer reaches the top mask
- As this is due to surface tension it again is concentrated around the air/polymer interface
- This is due to the small contact angle (20-30° for PDMS and the mask)

# The Model

- Process is modelled using the Lamina Phase Field and Electrostatics modules in COMSOL 4.0/4.2
- The Lamina Phase field module describes the motion of the fluid using Navier-Stokes and the surface using a Diffuse Interface Phase Field model
- The phase field module calculates the surface tension forces
- The Electrostatics module solves for the voltage and calculates electric field from this
- This electric field is then used to calculate the interfacial force due to the electric field

# Interfacial Force

- The charge density at the surface is represented by
- This is derived from the surface charge density in terms of the polarisation:

$$\sigma = \mathbf{P} \cdot \hat{\mathbf{n}}$$

- And the Polarisation in terms of the electric field

$$\mathbf{P} = (\epsilon_r - 1)\epsilon_0 \mathbf{E}$$

- This equation is then combined with the expression for electrostatic force:

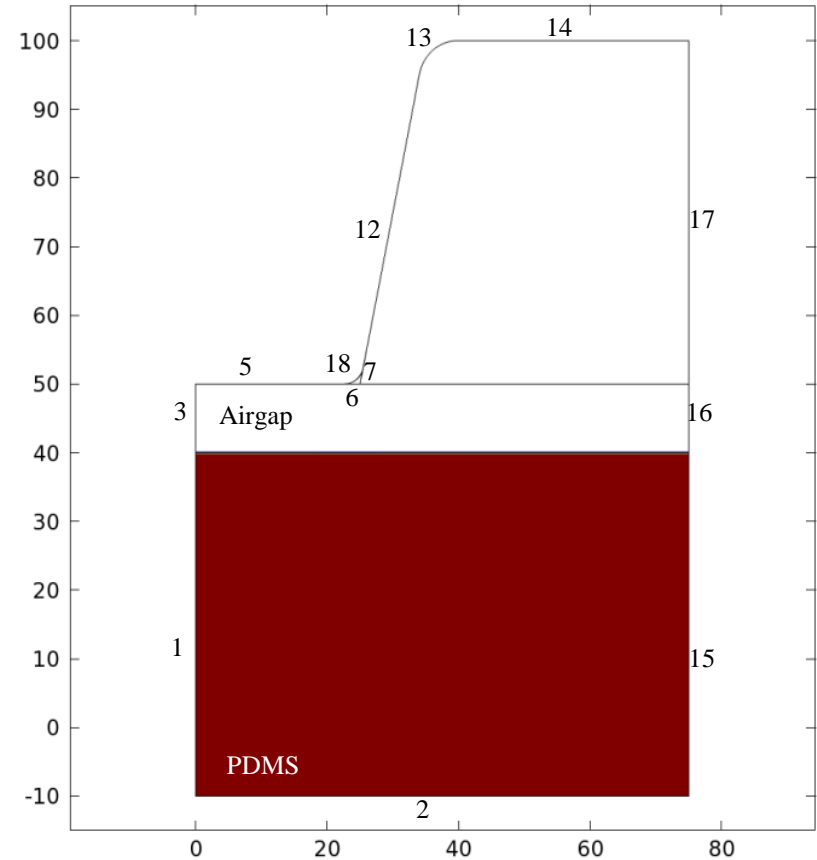
$$\mathbf{F} = \rho_f \mathbf{E} - \frac{1}{2} \mathbf{E} \cdot \mathbf{E} \nabla \epsilon + \nabla \left( \frac{1}{2} \mathbf{E} \cdot \mathbf{E} \frac{\partial \epsilon}{\partial \rho} \rho \right)$$

- To give an expression for the force per unit area at the interface:

$$\mathbf{F} = ((\epsilon_r - 1)\epsilon_0 \mathbf{E} \cdot \nabla \phi) \mathbf{E} - \frac{1}{2} \mathbf{E} \cdot \mathbf{E} \nabla \epsilon + \nabla \left( \frac{1}{2} \mathbf{E} \cdot \mathbf{E} \frac{\partial \epsilon}{\partial \rho} \rho \right)$$

# Geometry and Boundary Conditions

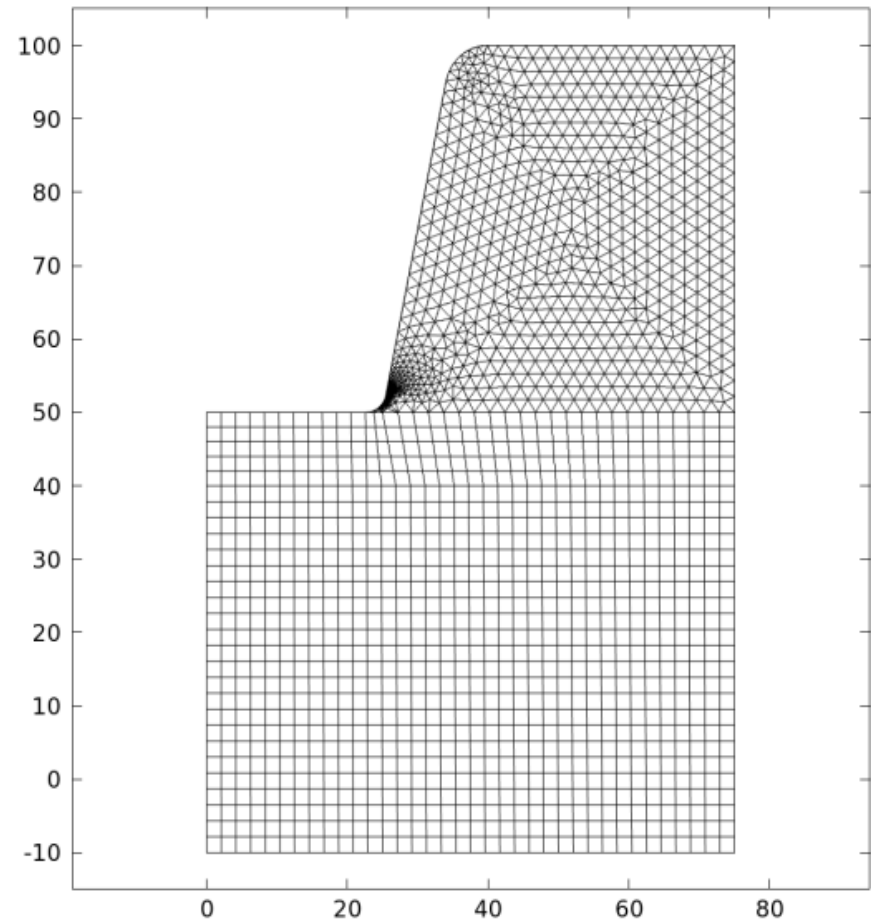
|    | Flow         | Electric Field |
|----|--------------|----------------|
| 1  | Slip Wall    | Symmetry       |
| 2  | No-Slip Wall | 0V             |
| 3  | Slip wall    | Symmetry       |
| 5  | Slip wall    | 300V           |
| 6  | Wetted Wall  | N/A            |
| 7  | Wetted Wall  | N/A            |
| 12 | Wetted Wall  | 300V           |
| 13 | Wetted Wall  | 300V           |
| 14 | Wetted Wall  | 300V           |
| 15 | Symmetry     | Symmetry       |
| 16 | Symmetry     | Symmetry       |
| 17 | Symmetry     | Symmetry       |
| 18 | N/A          | 300V           |



# Mesh and Material properties

- Triangular Elements are used in the top part of the mask
- Mapped Quads are used in the lower part
- Material Properties

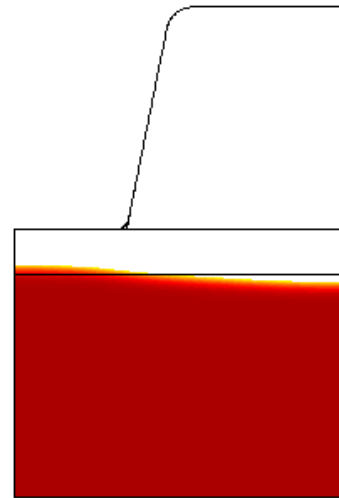
| Simulation Dynamic Viscosity (Centipoise) | Specific Gravity (25°C) | Dielectric Constant (100Hz) | Surface Tension (mN/m) |
|---|-------------------------|-----------------------------|------------------------|
| 1000                                      | 1.03                    | 2.72                        | 20                     |



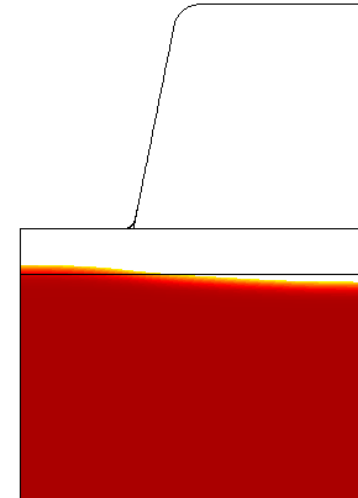


# Viscosity

- To reduce simulation time a lower viscosity has been used
- These animations compare a 250 cp case to a 1000 cp case
- The final thickness is the same only the simulation time is different



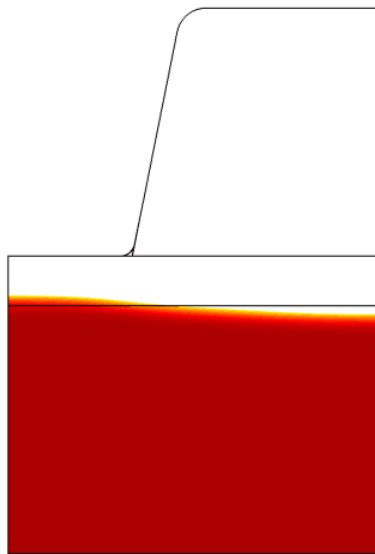
250 cp



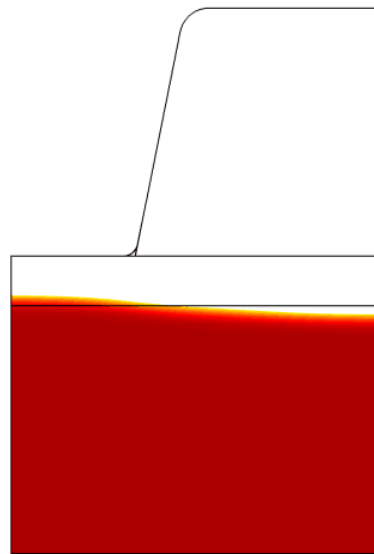
1000 cp

# Effect of Contact Angle

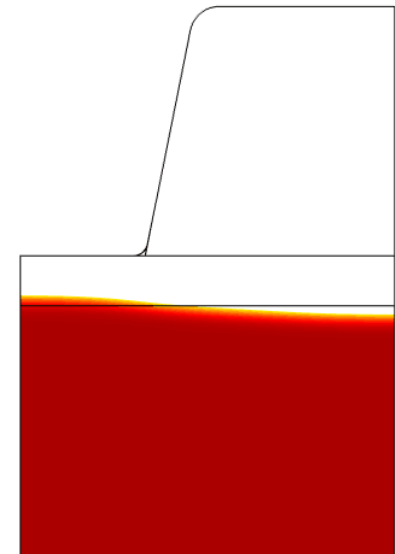
- Increasing Contact angle Decreases Cap Thickness



10° contact Angle



20° contact Angle

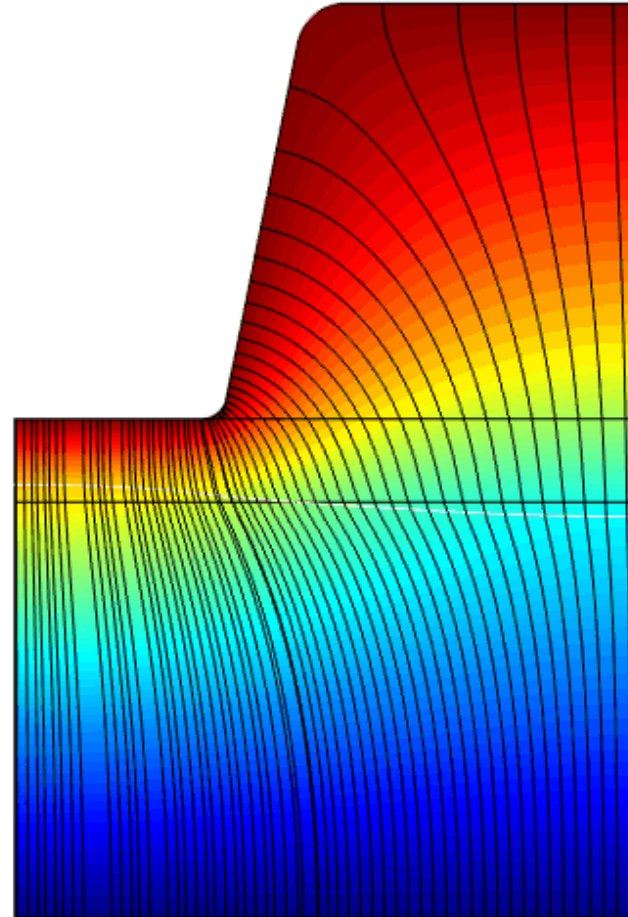
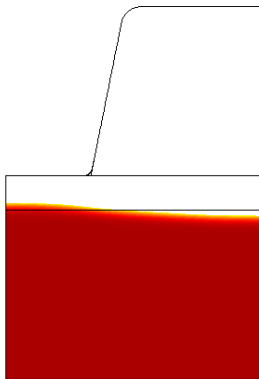


25° contact Angle  
Unable to form Complete Cap

- This is probably due to the reduced capillary force

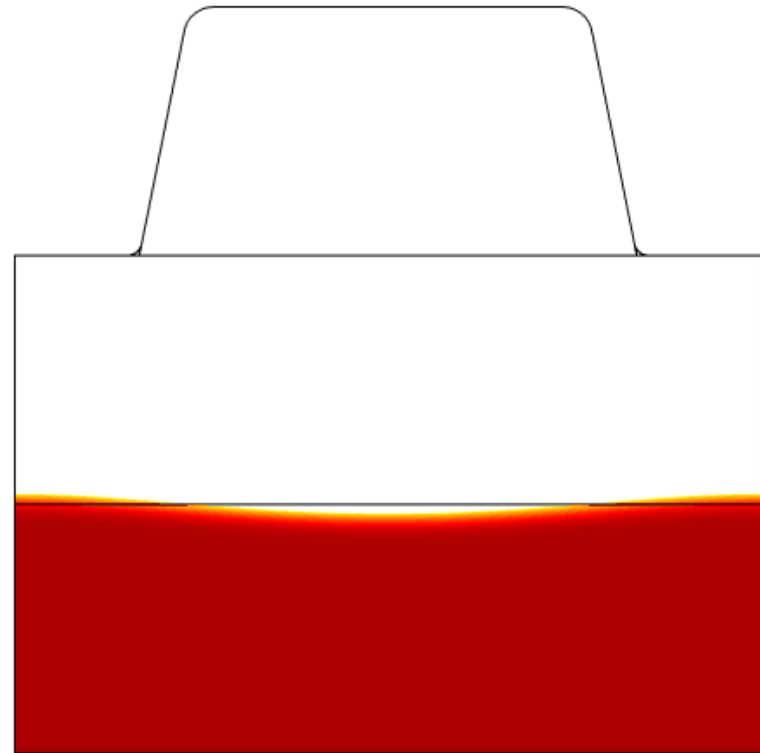
# Electric Field

- Electric field at the surface (white line) is higher under the lower part of the mask
- This is what causes the surface to move

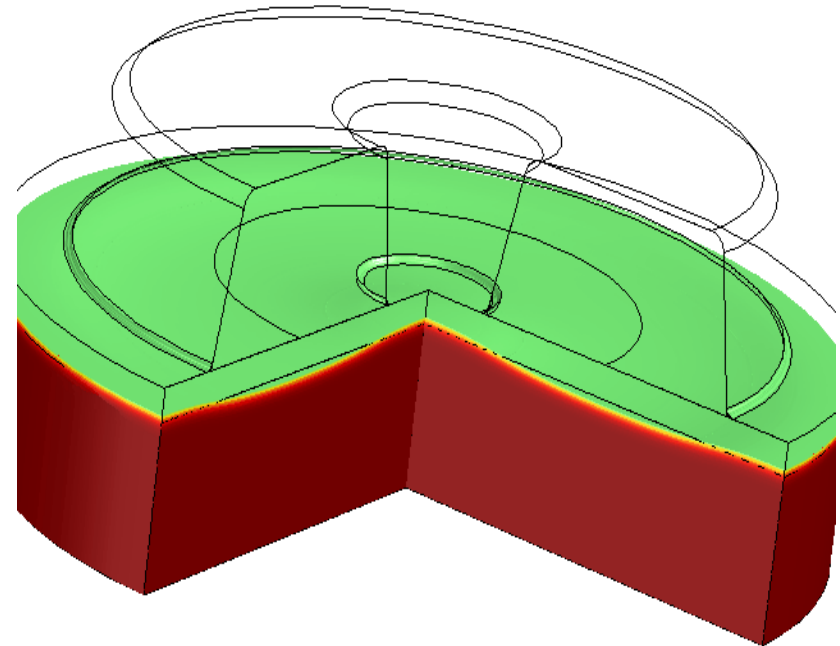
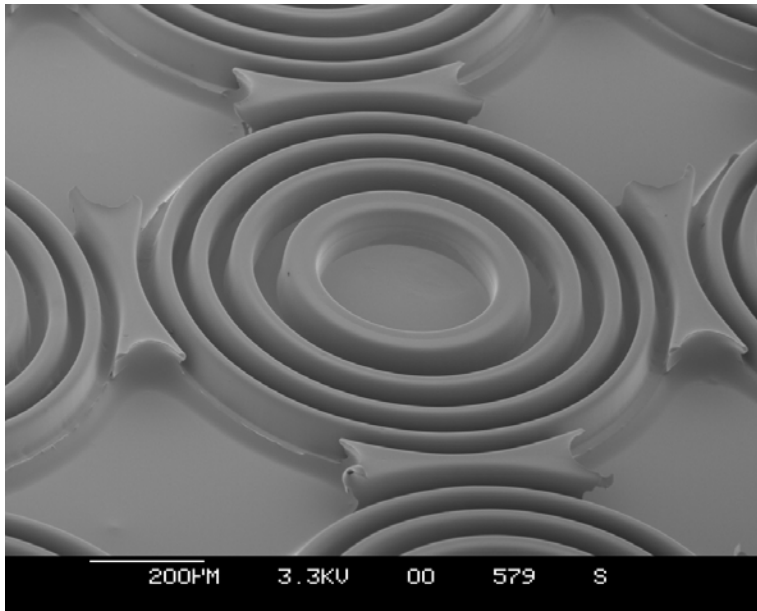


# Large Air Gap

- Increasing the Air Gap creates a deeper channel for the same amount of polymer
- Using a wetted surface at the bottom results in a square bottomed channel



# Comparison with Experiment



Angled Channel 15° contact Angle  
Swept to form a 3D representation

# Conclusions

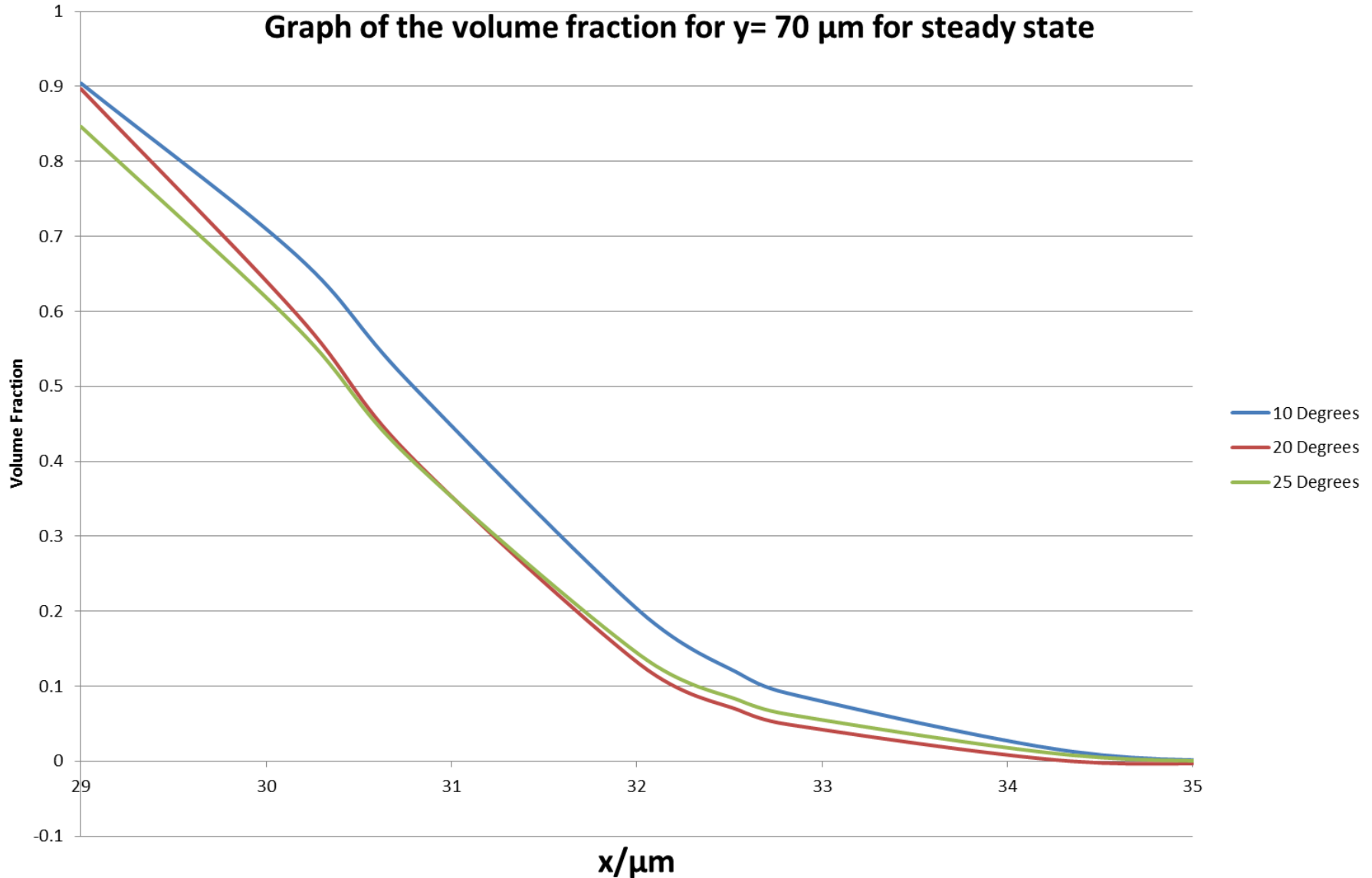
- The model presented here has provided some further avenues for further investigation
- The main one of these in terms of reliability is contact angle which should be alterable by changing the mask properties
- Further work is needed to develop a model including higher viscosities and also incorporating a Oldroyd-B model of the viscoelasticity, to see if this has an effect on the shape of the structures

# Thank You

Any Questions?

# Contact Angle

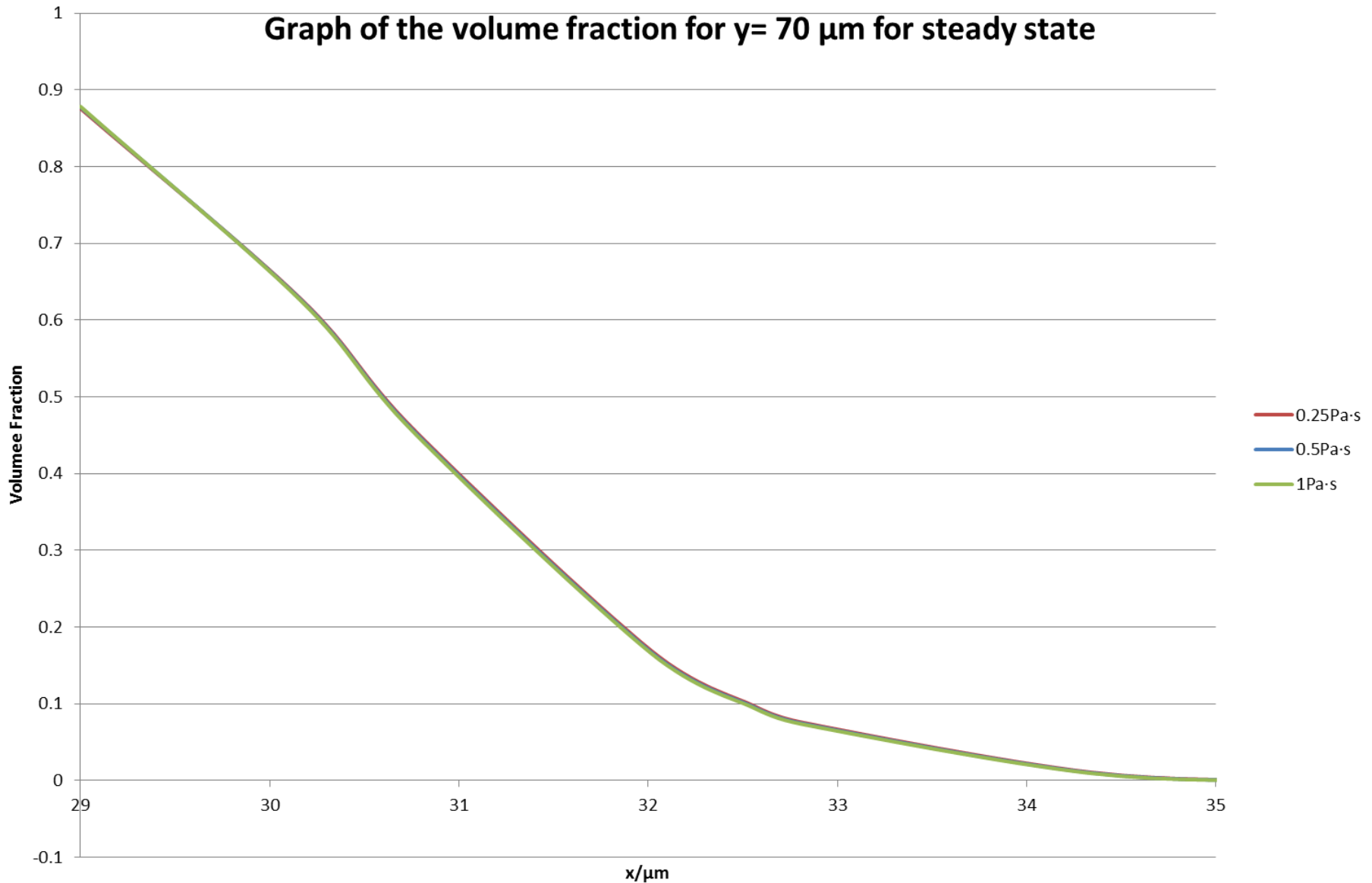
Graph of the volume fraction for  $y = 70 \mu\text{m}$  for steady state





# Viscosity

Graph of the volume fraction for  $\gamma = 70 \mu\text{m}$  for steady state



# Viscosity – Difference from 1Pa·s

