

# High Frequency Resonators using Exotic Nanomaterials

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### Introduction:

- Recent innovations in area of 1-D and 2-D nanomaterials has resulted in significant interest in the use of such materials for metrology, mass sensing, biosensing, telecommunication, and high frequency resonator applications.
- While important, it may be time consuming and prohibitively expensive to characterize them all experimentally.
- COMSOL multi-physics models could potentially be useful to characterize these materials as high frequency devices for future applications.

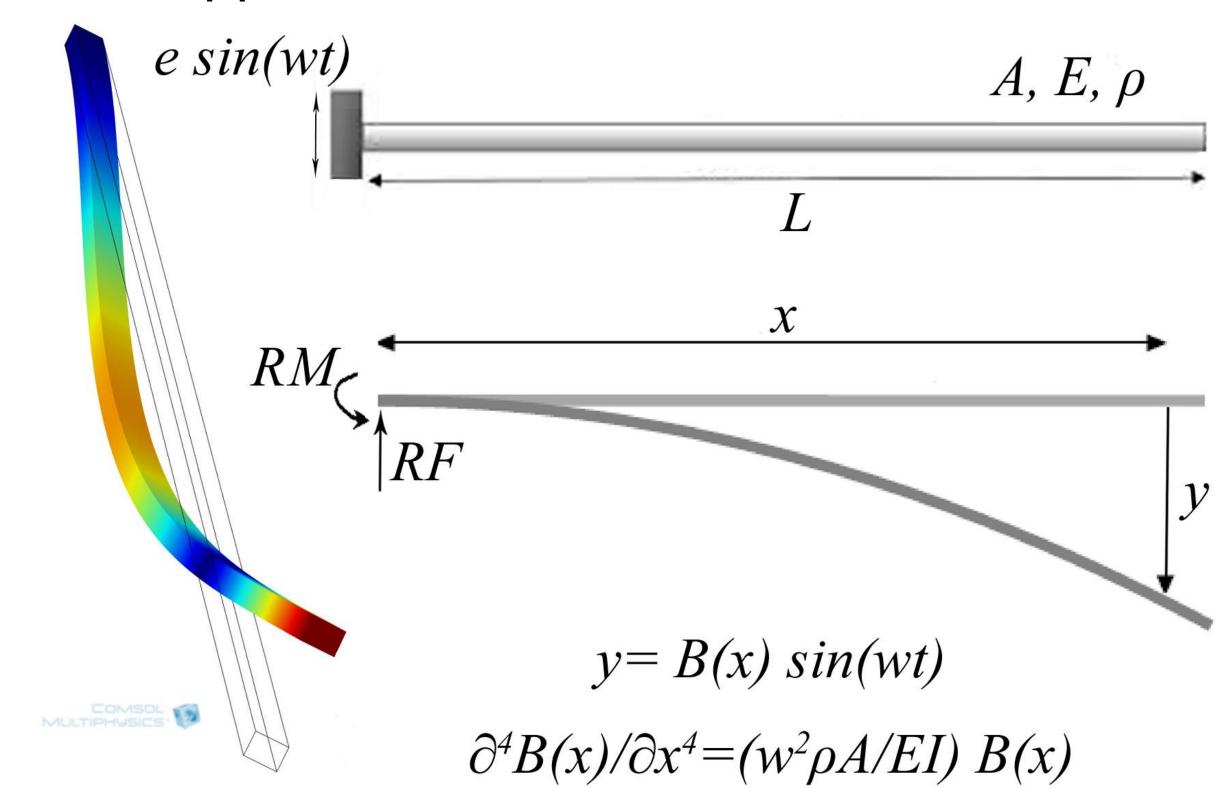
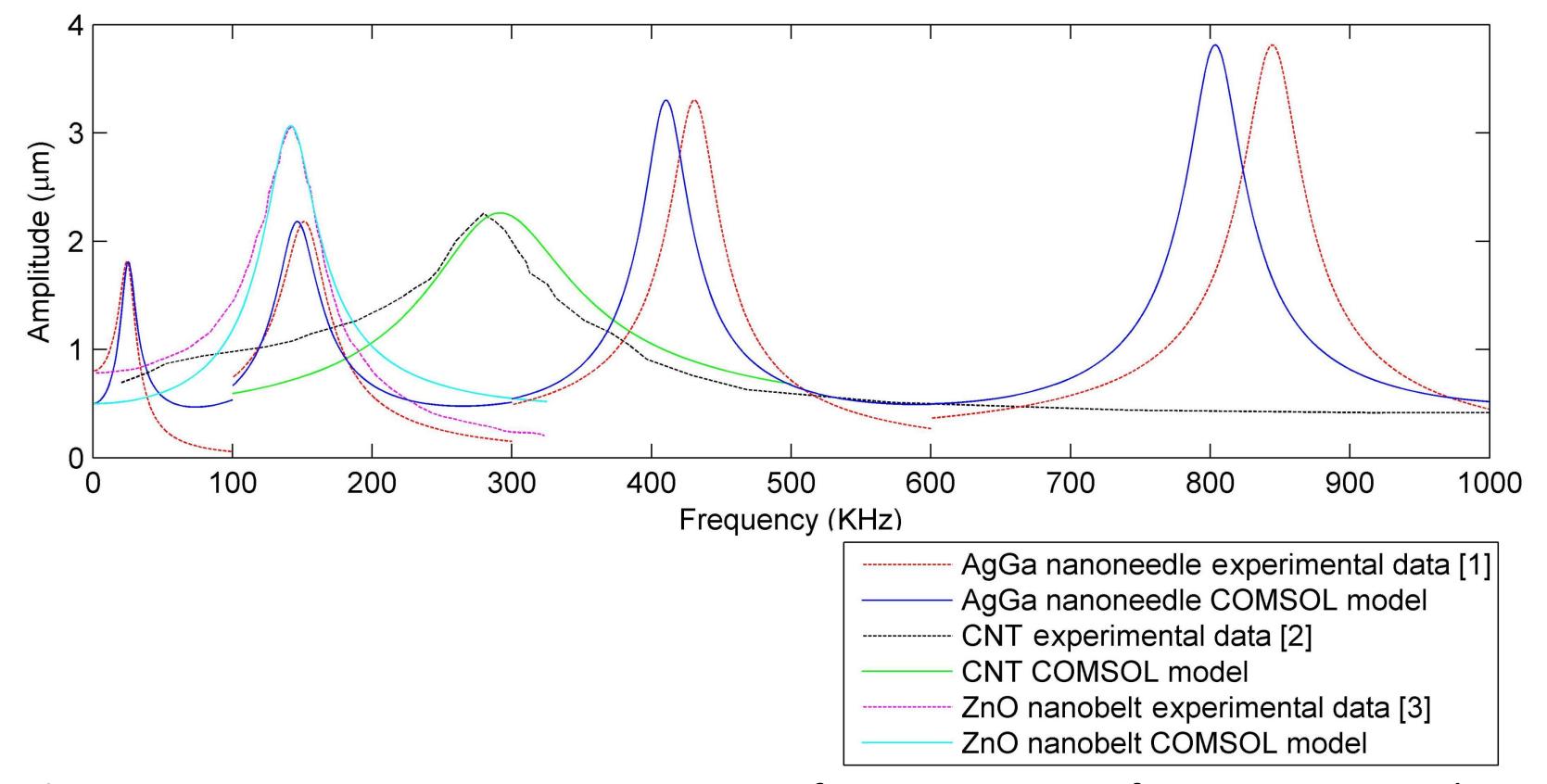


Figure 1. Nanoresonator model as an Euler-Bernoulli beam

## **Computational Methods:**

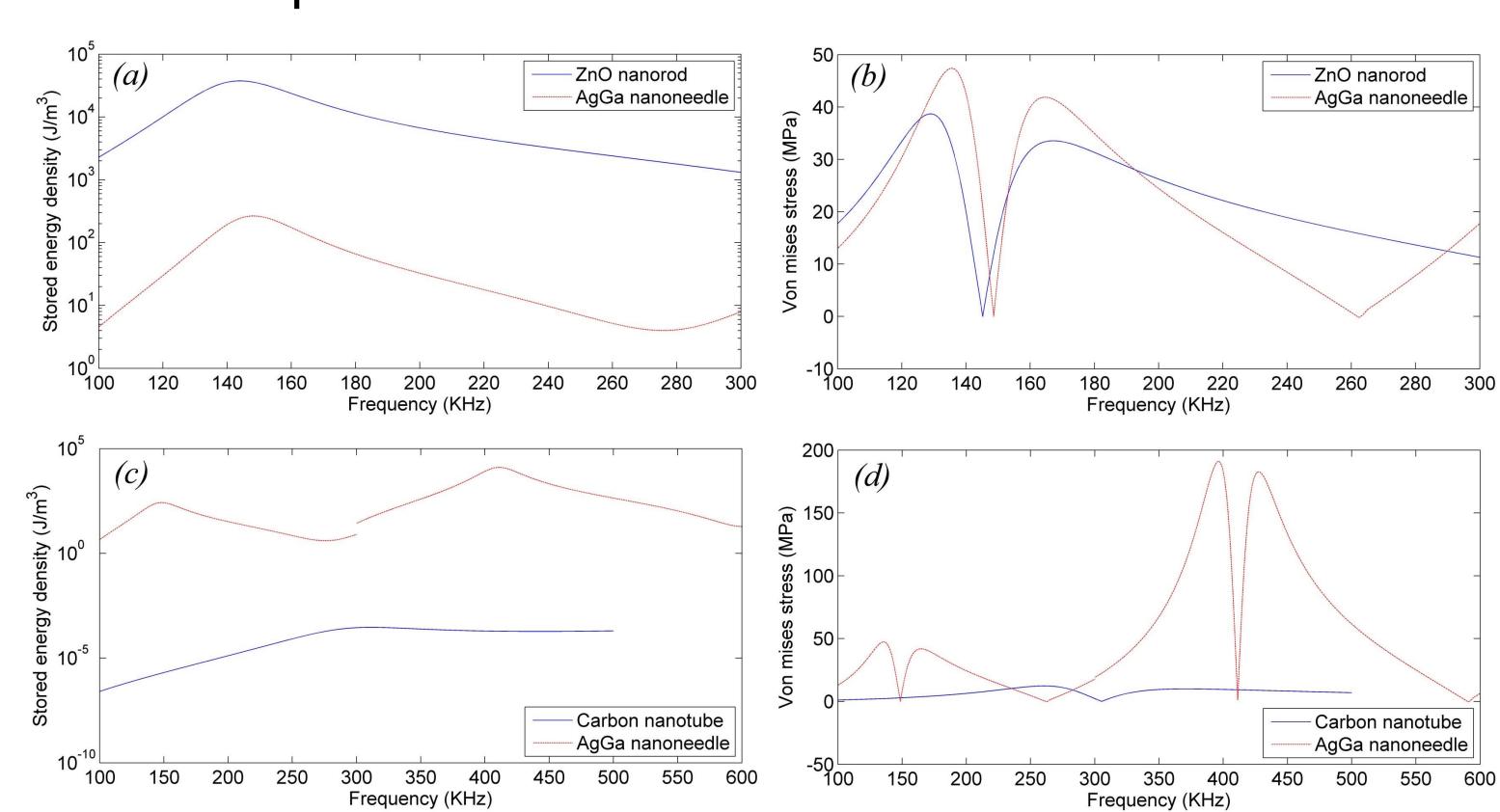
- Instead of beam element, we used structural mechanics module using 3D cubic element that is elongated along the axis of the beam in COMSOL.
- Clamp-free was considered as the boundary conditions of the beam and base motion vibration with ~500 nm amplitude at the clamp end was applied as the input.
- Mechanical damping function was imported into the model by defining loss factor that was equal to inverse of quality factor of resonator.
- We compared experimental data on Ag<sub>2</sub>Ga nanowires, carbon nanotube, and ZnO nanoresonators to validate this model.



**Figure 2.** Frequency response comparison of nanoresonators from experimental data and COMSOL.

#### Results:

- Figure 2 compares the results of COMSOL model with data reported in references [1-3]. The experimental peaks were normalized to their relevant simulations peaks from COMSOL.
- The resonance frequencies from COMSOL simulation were in match with the experimental data and the maximum difference in resonance frequencies was within ~4.1% (Ag<sub>2</sub>Ga 4<sup>th</sup> mode).
- The first mode of ZnO nanobelt had higher vibration amplitude at the tip, higher stored elastic energy (Fig 3a), and lower stress at the clamp end in comparison to 2<sup>nd</sup> mode of Ag<sub>2</sub>Ga nanoneedle (Fig 3b).
- Also, CNT had very low stress at the clamp end (Fig 3d), however its stored elastic energy was low (Fig 3c) in comparison to the other two nanoresonators.



**Figure 3**. Comparison of stored energy and von Mises stress at the clamping end for different nanoresonators.

# Conclusions:

- The presented COMSOL model is developed to simulate the frequency response of nanoresonators with different geometries (cubic, cylindrical, tube) for various materials (ZnO, Ag<sub>2</sub>Ga, CNT).
- COMSOL results for nanoresonators are in good match with experimental data and it can be used to predict the behavior of other exotic materials including graphene, MoS<sub>2</sub>, nanodiamond, BN, SiC and others.
- Among the materials studied here, ZnO nanobelt is a wonderful candidate as a mechanical nanoresonator.

# Acknowledgements:

Funding for this work was provided by NSF ECCS: 1202190

## References:

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- 3. K. Yum etc., "Experimental measurement and model analysis of damping effect in nanoscale mechanical beam resonators in air," *Journal of Applied Physics*, vol. 96, pp. 3933-3938 (2004)