



COMSOL  
CONFERENCE  
2014 CAMBRIDGE

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# Prediction of Noise Generated by Electromagnetic Forces in Induction Motors

# Presentation Outline

- Introduction and Background
- Motor Components
- Model development for magnetic noise
  - Electromagnetic Model
  - Mechanical and Acoustic Models
  - Prediction Results
- Conclusion

# Product and System Examples

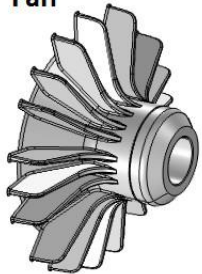


# Main Components in Induction Motors

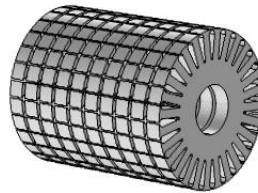
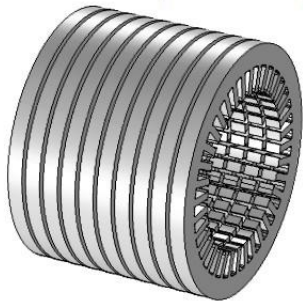


Squirrel cage motor with straight bars

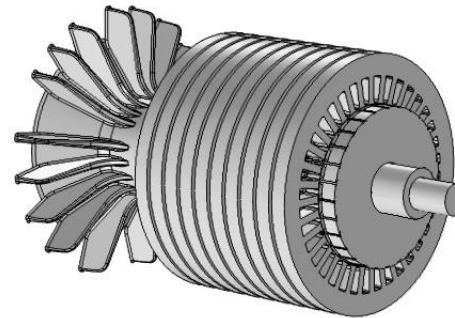
Fan



Stator Core  
(Laminated)



Rotor Core  
(Laminated)



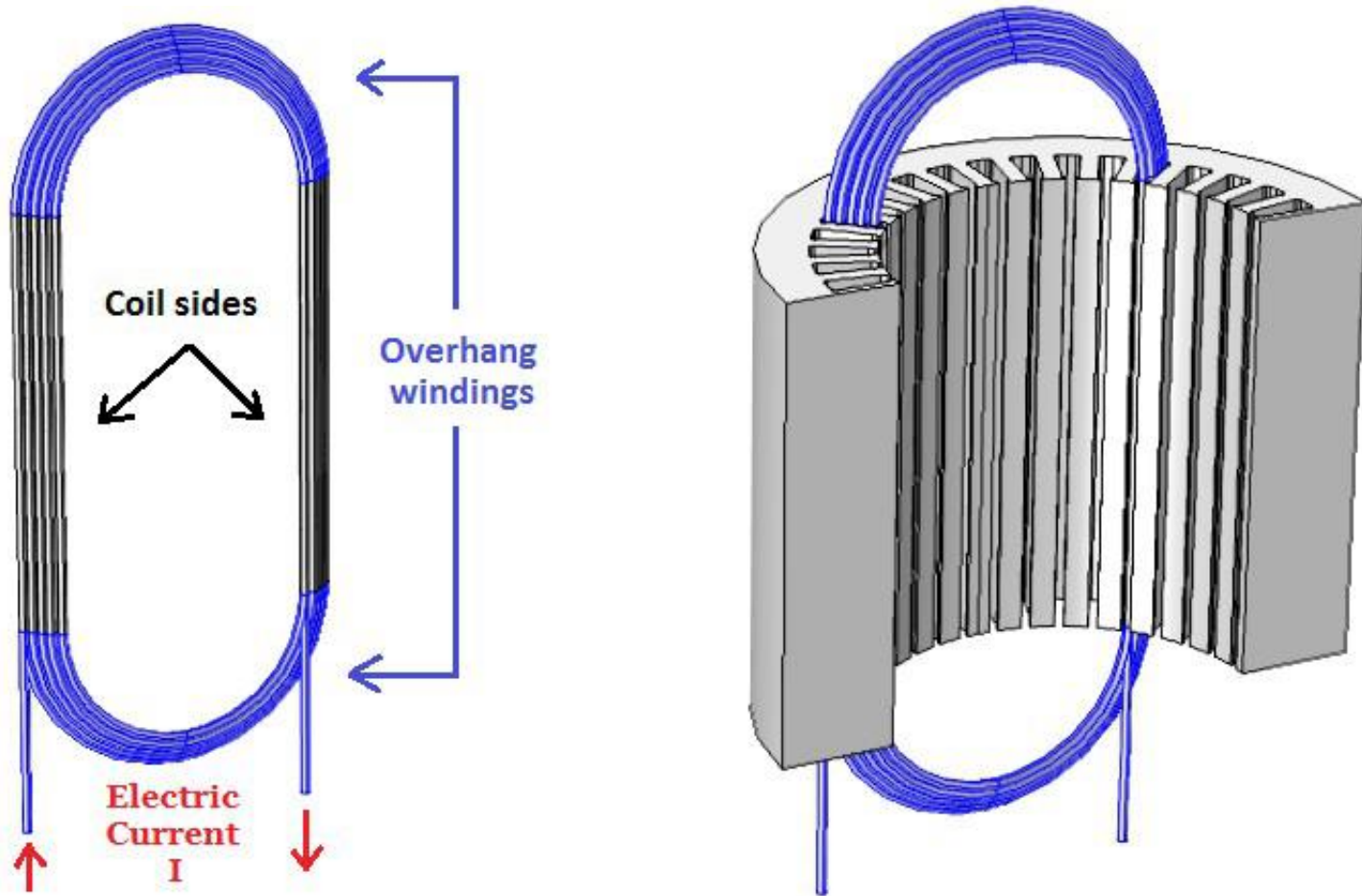
Rotor Cage

Shaft





# Motor Windings or Coils

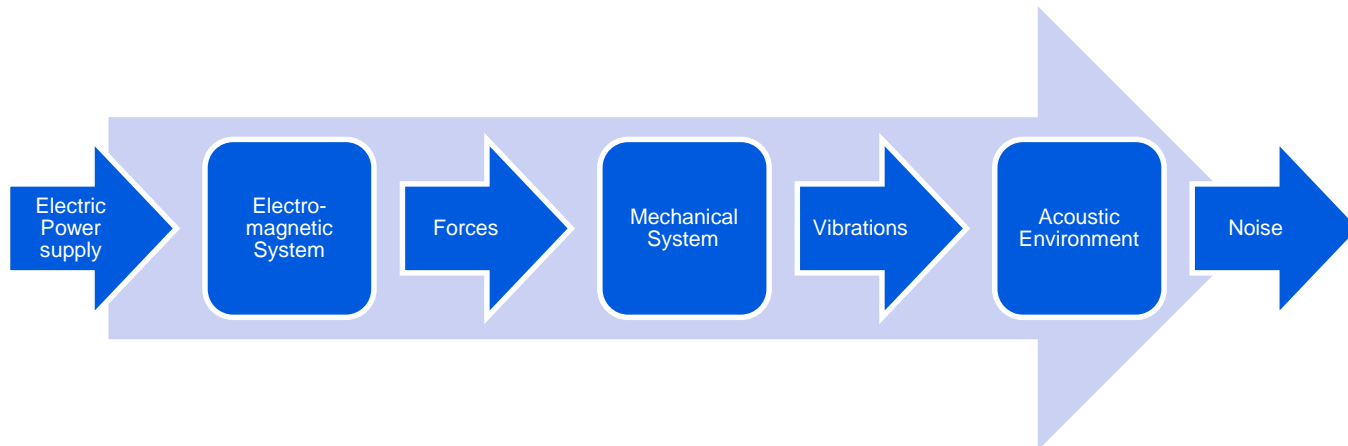


# Motor Acoustics

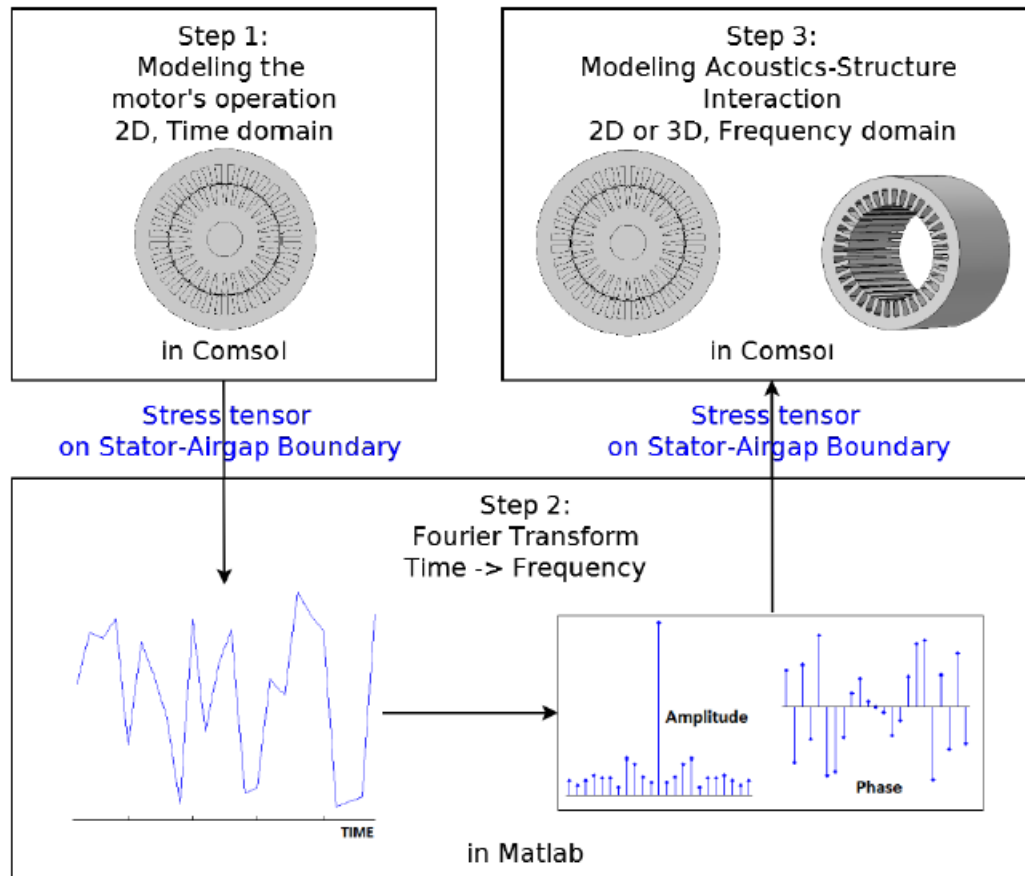
## Noise Sources

- 1) Magnetic Noise
- 2) Fan Noise
- 3) Mechanical Noise

## Energy Conversion Chain from electric supply to noise

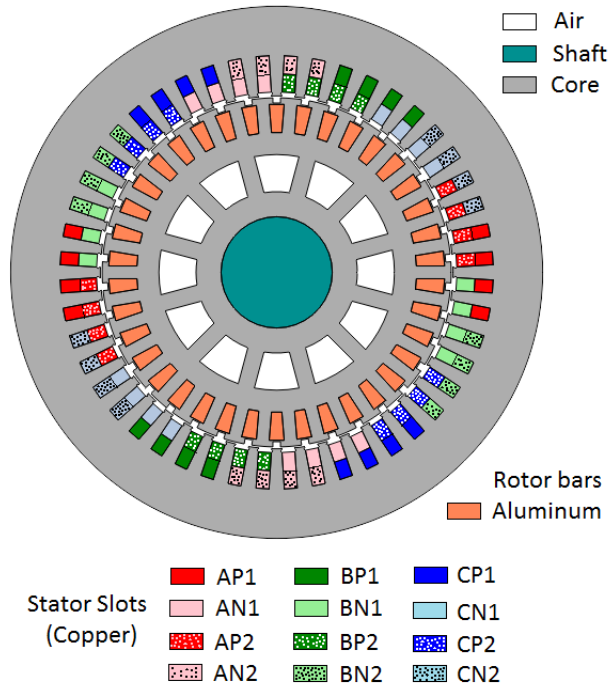


# Model Building Procedure

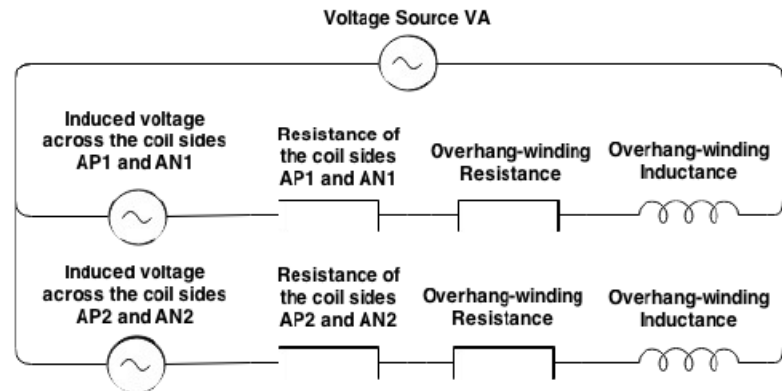


# Stator Winding and Equivalent Circuit

The equivalent circuit: Lumped Model



The stator circuit for one phase

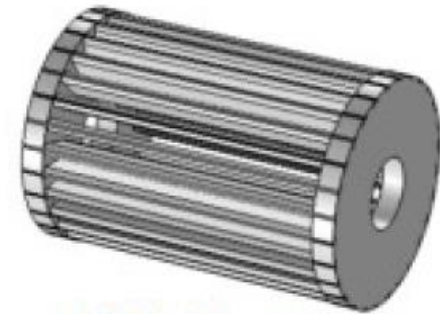
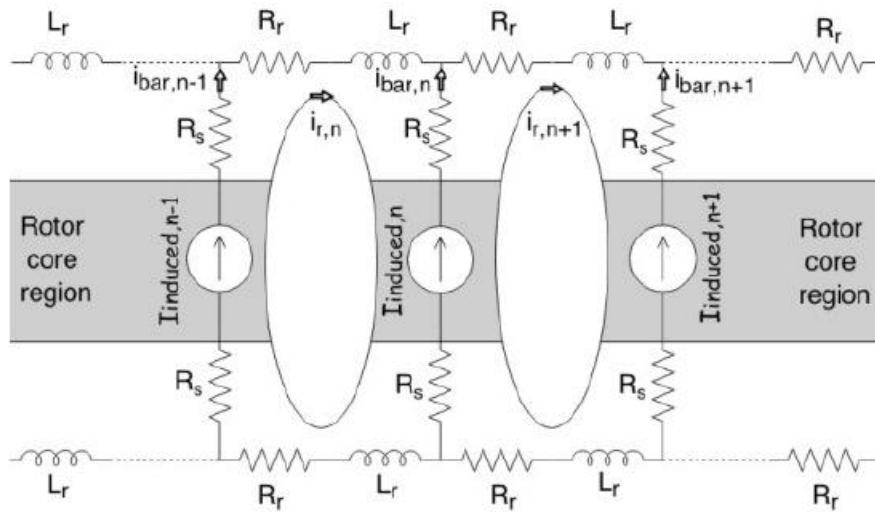


- 48 slots
- 38 bars
- 2 branches for each phase circuit



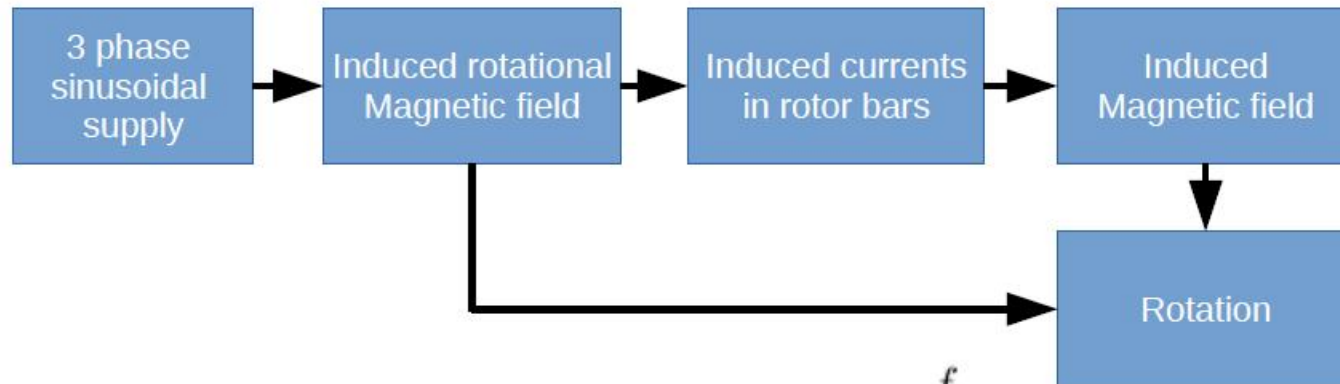
# Equivalent Circuit for Rotor

The equivalent circuit: Lumped Model



**Rotor Cage**

# Induction Motor in Operation



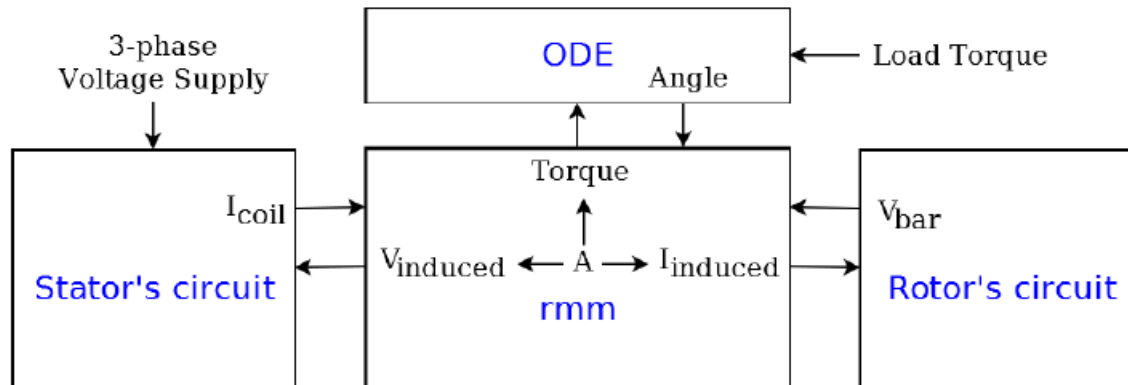
- Synchronous speed  $n_{ss} = 120 \times \frac{f}{n_P}$
- Slip  $s = \frac{n_{ss} - n_{rs}}{n_{ss}} \times 100$

*Motor 1*  $f = 50Hz, n_p = 4 \rightarrow 1500rpm$

$f$  : supply frequency (Hz)  
 $n_P$  : number of poles

$n_{ss}$  : synchronous speed (rpm)  
 $n_{rs}$  : rotational speed of the rotor (rpm)

# Step 1: Electromagnetic Model



Solve for:  
A, I<sub>coil</sub>,  
V<sub>bar</sub>, Angle

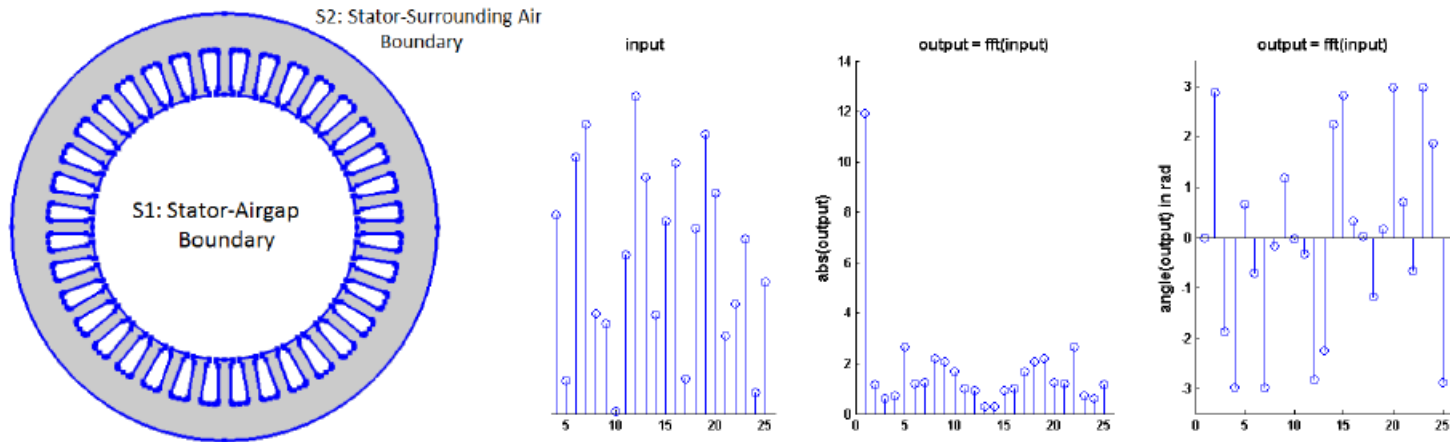
- Lamination is perfect → no eddy current loss
- Coils are made of thin wires and perfectly insulated from one another

$$\nabla \times (\nu \nabla \times \mathbf{A}) = \begin{cases} N_w I_w \mathbf{e}_z / S_w & \text{in stator slots} \\ -\sigma \frac{\partial \mathbf{A}}{\partial t} + \sigma V_b \mathbf{e}_z / l_b & \text{in rotor bars} \\ -\sigma \frac{\partial \mathbf{A}}{\partial t} & \text{in shaft} \\ 0 & \text{elsewhere (cores, airgap)} \end{cases} \quad (3.17)$$

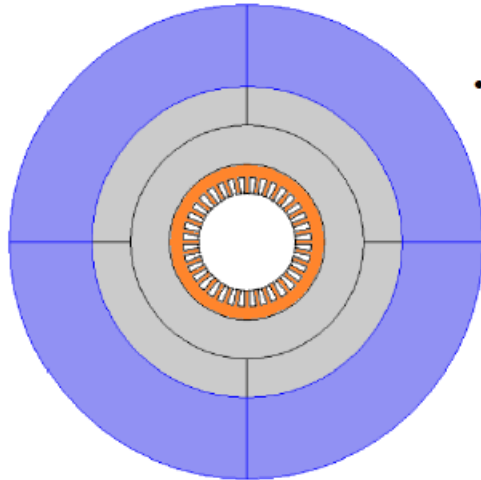
$$J \frac{d^2 \alpha}{dt^2} = \mathbf{T}_{\text{rotor}} - \mathbf{T}_{\text{load}} \quad (3.29)$$

# Step 2: Transformation from Time to Freq. Domain

- Extract Maxwell stress tensor along the Stator-Airgap Boundary during the steady state
- Transform from time to frequency domain using Fast Fourier transform in Matlab
- Save the results in text files for next step



# Step 3: Acoustics and Mechanical Models



- Stator core (iron)
- Surrounding air layer
- Perfectly matched layer (air)

- Young modulus: stress-strain
- Poisson ratio: strain-strain

- Stator + Surrounding air + PML (air)
- The air density is unchanged in time & space

$$\rho_S \ddot{\mathbf{u}} = \nabla \cdot \boldsymbol{\sigma} + \mathbf{F}_V \quad \text{in stator}$$

$$\ddot{p} - c^2 \nabla \cdot (\nabla p) = 0 \quad \text{in air}$$

$$\frac{1}{\rho_A} \mathbf{n} \cdot (\nabla p) = -\mathbf{n} \cdot \ddot{\mathbf{u}} \quad \text{in Stator-Air boundary}$$

$$\boldsymbol{\sigma} \cdot \mathbf{n} = p \mathbf{n} \quad \text{in Stator-Air boundary}$$

$$-\rho_S \omega^2 \mathbf{u} = \nabla \cdot \boldsymbol{\sigma} + \mathbf{F}_V \quad \text{in stator}$$

$$-\omega^2 p - c^2 \nabla \cdot (\nabla p) = 0 \quad \text{in air}$$

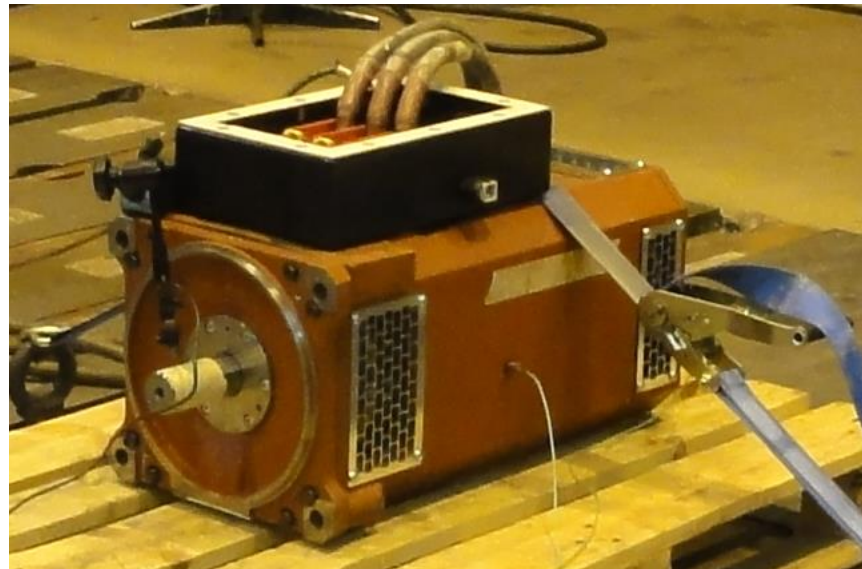
$$\frac{1}{\rho_A} \mathbf{n} \cdot (\nabla p) = -\omega^2 \mathbf{n} \cdot \mathbf{u} \quad \text{in Stator-Air boundary}$$

$$\boldsymbol{\sigma} \cdot \mathbf{n} = p \mathbf{n} \quad \text{in Stator-Air boundary}$$

$\omega (= 2\pi f)$  is the angular frequency (in *rad/s*)

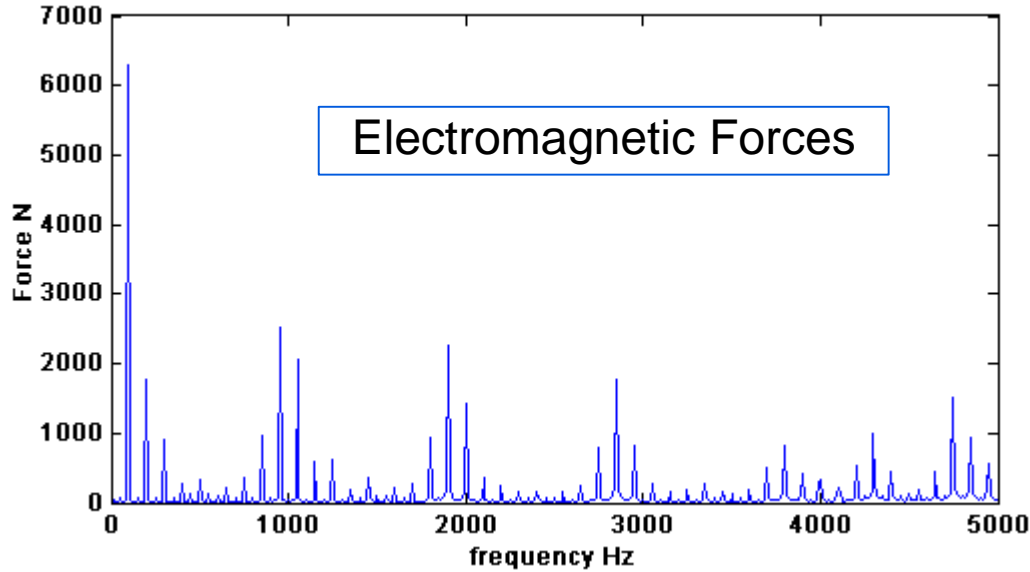
# Motor Parameters

Power supply	3 phase, 388V (nominal)
Number of poles	4 poles
Stator	48 slots
Rotor	Squirrel cage, 38 straight bars
Load	No load

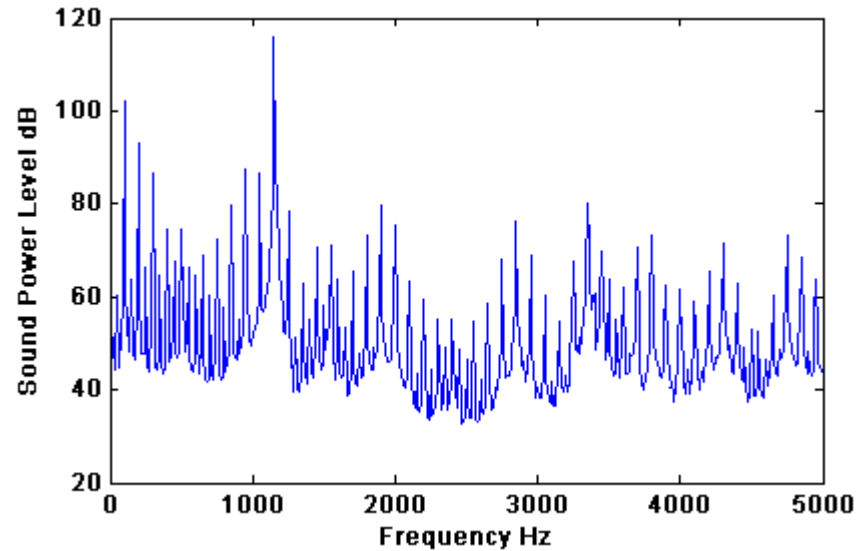




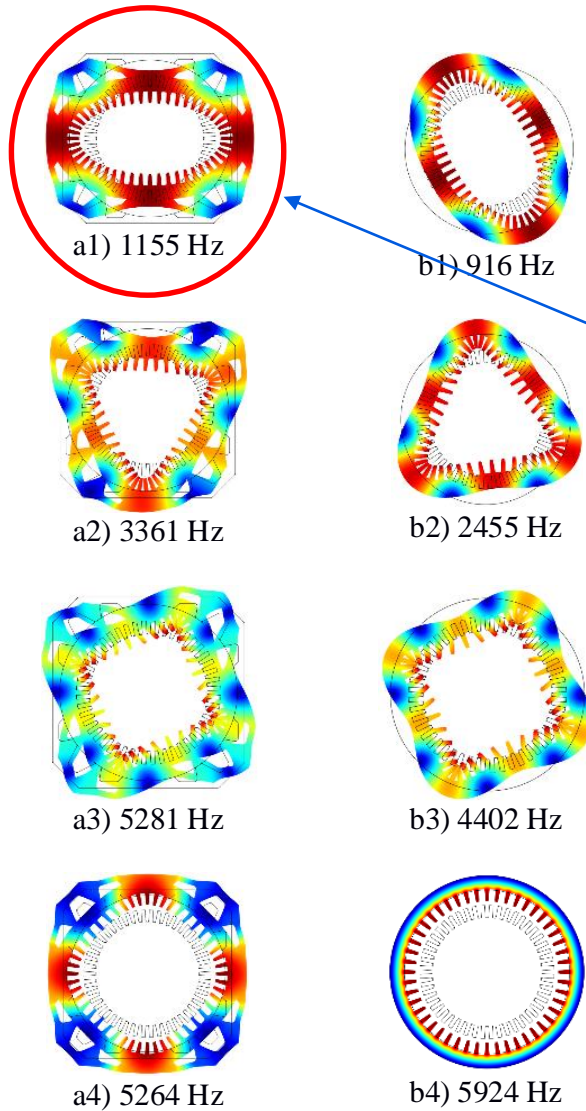
# Prediction Results



Sound Power Level



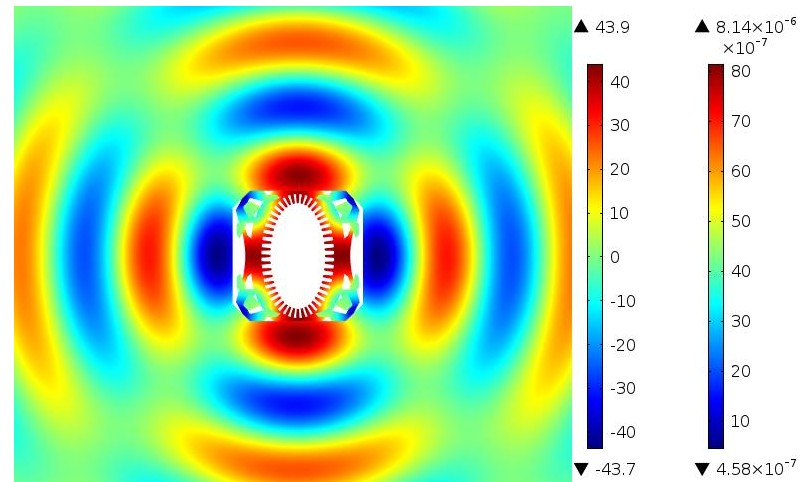
# Structural Resonances



Mode Shapes of stator with housing

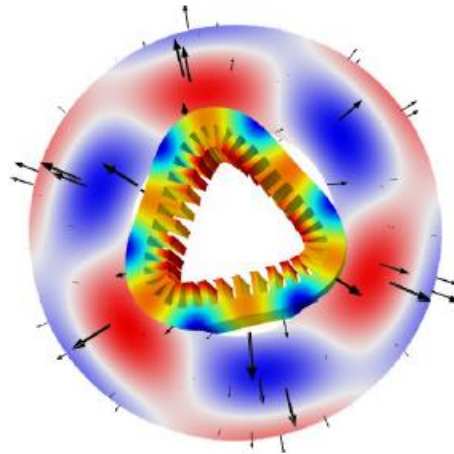
Particular resonance interacting with the electromagnetic excitation

Sound Radiation Pattern at 1155 Hz



# Conclusion

- A multiphysic model to predict magnetic noise was built in COMSOL
- The electromagnetic model of the motor in 2D is solved in time domain
- The resulting electromagnetic forces are used in the frequency domain to perform the mechanical and acoustic analysis in 2D
- Future work on a 3D structural model and implementation of BEM for sound propagation



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