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Multiphysics Analysis of RF Cavities for Particle Accelerators: Perspective and Overview

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Particle Accelerators: Why?

High Energy Physics

- Standard Model
- Matter and Anti Matter
- Symmetry Violation

Medical Applications

- Medical Isotopes
- Cancer Therapy
- Analyze and define how the ribosome translates DNA information into life (DNA research)

Industrial Applications

- Implant ions in silicon chips (Semiconductor industry)
- Analyze protein structures, leading to the development of new drugs to treat major diseases such as cancer, diabetes, malaria and AIDS

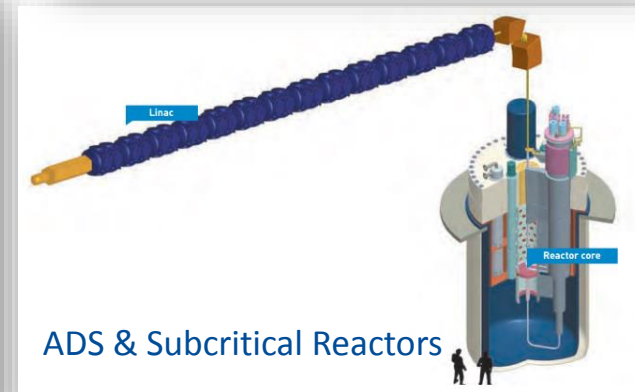
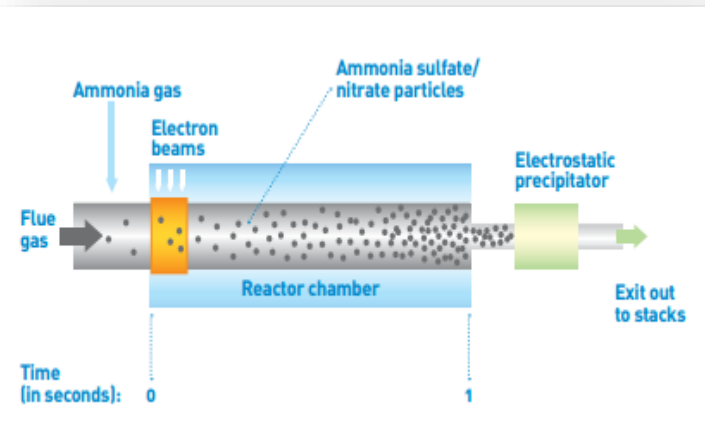
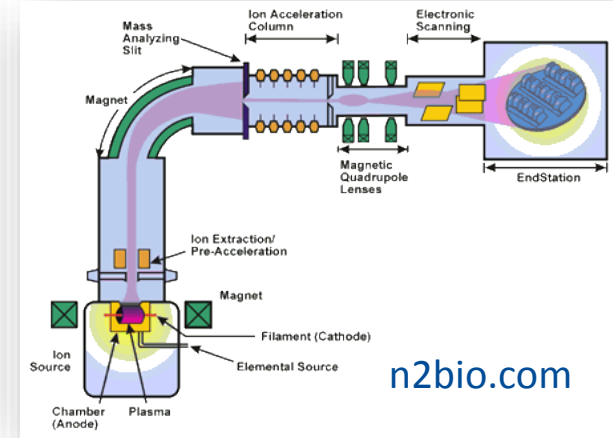
Nuclear Applications

- Nuclear Waste Transmutation
- Nuclear Energy Production with Alternative Fuel
- Radio Isotopes

Environmental Applications

- Clean up dirty water, sewage sludge and polluted gases from smokestacks.

Particle Accelerator: Why?



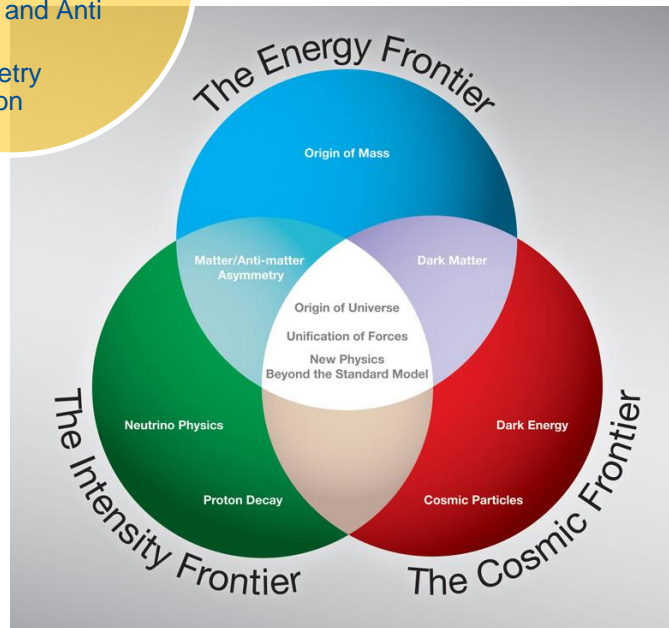
Accelerators for Americas Future, <http://science.energy.gov/~media/hep/pdf/accelerator-rd-stewardship/Report.pdf>

Fermi National Accelerator Laboratory

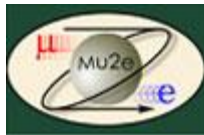
Fermilab is a main player in the High Energy Physics Research

High Energy Physics

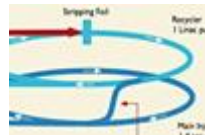
- Standard Model
- Matter and Anti Matter
- Symmetry Violation



LBNF



Mu2e



PIP-II



NOVA



μ BooNE



MICE



DE Survey Telescope



LSS Telescope

Classification of Particle Accelerators

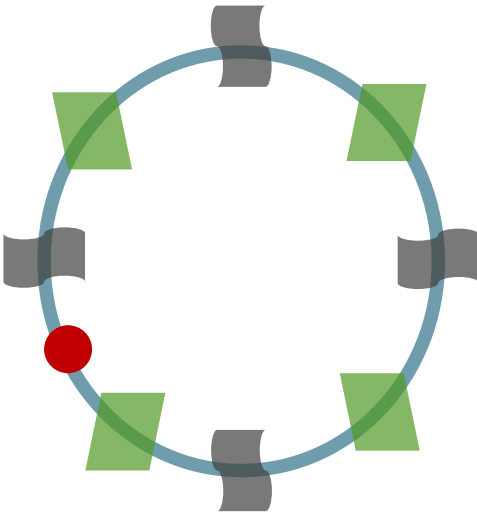
$$F = q(E + v \times B)$$

Electric field for acceleration

Magnetic field for bending/focusing

Cyclic

Linac



- Tunable RF Cavities
- Bending and Focusing Magnets

- Fixed Frequency RF Cavities
- Focusing Magnets



Cyclotron

- Fixed f
- Fixed B
- Variable R

Syncho-cyclotron

- Variable f
- Fixed B
- Variable R

Synchrotron

- Variable f
- Variable B
- Fixed R

RF Cavities for Particle Accelerators



Normal-conducting Cavities

- Copper
- $Q \sim 1e4$
- $R_s \sim m\Omega$
- Room Temperature
- Power loss $\sim 10k$ Watts
- Gap Voltage $\sim 10kV$
- Limited by electromagnetic heating

Super-conducting Cavities

- Niobium
- $Q \sim 1e10$
- $R_s \sim n\Omega$
- $\sim 2K$
- Power loss \sim Watts
- Gap voltage $\sim MV$
- Limited by either field emission (surface cleanliness) or quench due to surface magnetic field (cavity loses its superconductivity)

Needed
Multiphysics

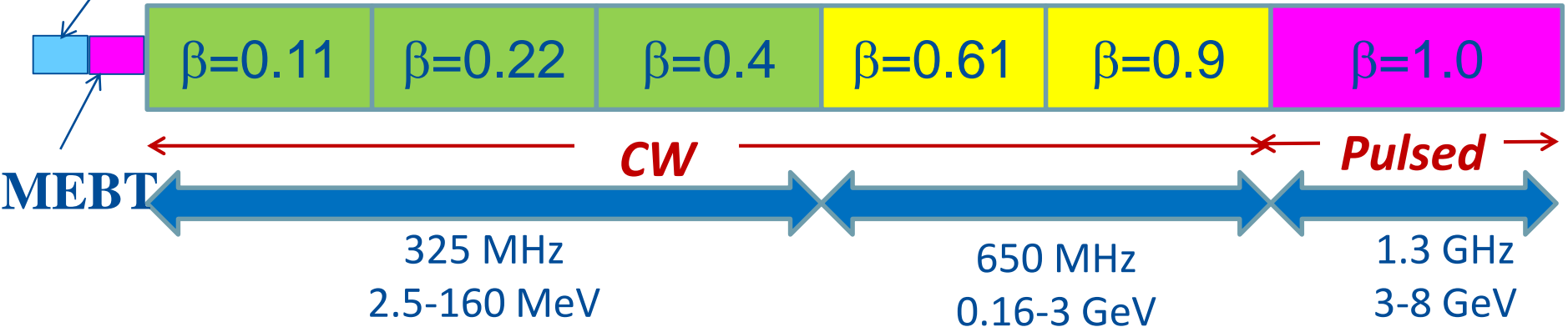
Eigenfrequencies
Electromagnetic
Heating, Frequency
Shifts

Eigenfrequencies
Mechanical Vibrations,
Frequency Shifts,
Thermal Quench

6

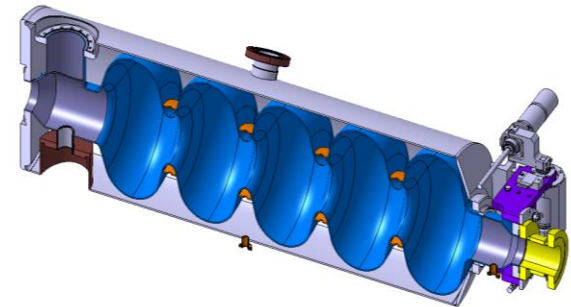
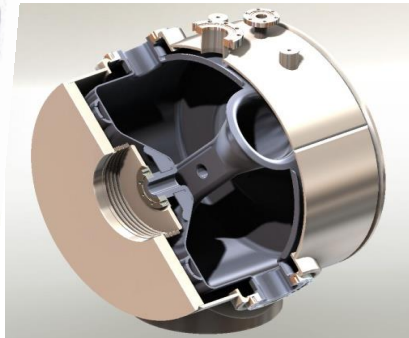
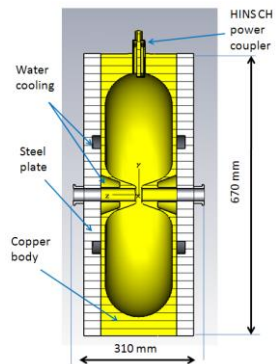
Typical SRF Linac

Ion source, RFQ



Low β Cavities

High β Cavities

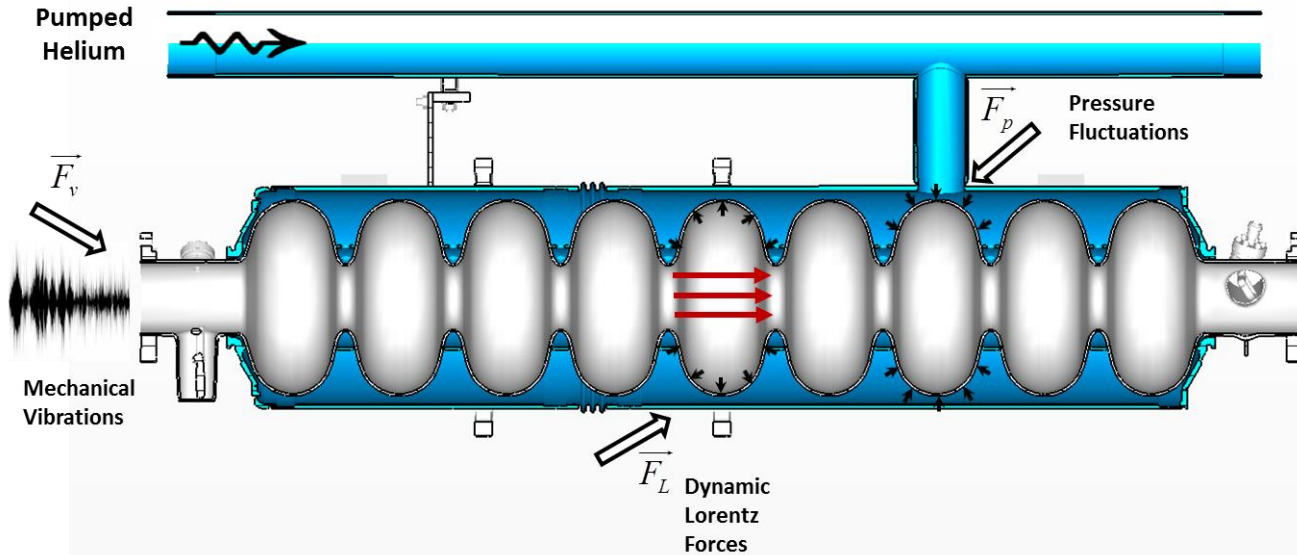


ReBuncher Cavity HWR

SSR

Elliptical Cavity

Sources of Frequency Detuning in SRF Cavities



Mechanical Vibrations

- Mechanical vibration that is already exist in the cavity system due to pumps and motors travel through the pipes and reach the cavity.
- Random effect

Pressure Fluctuations

- Helium pressure in the cryogenic system inherently fluctuates causing continuous pressure fluctuations on the cavity walls which induces detuning to the resonant frequency

Lorentz Force Detuning

- Electromagnetic fields inside the cavity exerts forces on the cavity wall that is proportional to the electric and magnetic energy

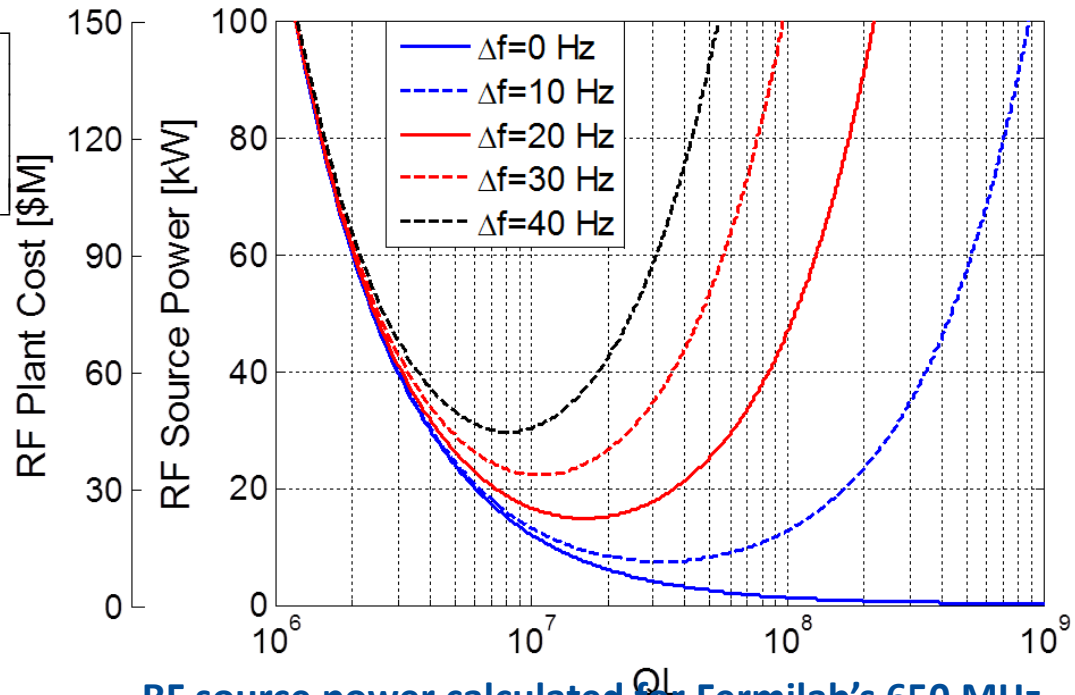
Significance of Minimizing Frequency Detuning

$$P_g = \frac{V_{cav}^2}{4 \frac{r}{Q} Q_L} \left[\left(1 + \frac{\frac{r}{Q} Q_L I_b}{V_{cav}} \cos(\Phi_b) \right)^2 + \left(\frac{\Delta f}{f_{1/2}} + \frac{\frac{r}{Q} Q_L I_b}{V_{cav}} \sin(\Phi_b) \right)^2 \right]$$

$$I_b = 0, P_g = \frac{V_{cav}^2}{4 \frac{r}{Q} Q_L} \left[1 + \left(\frac{\Delta f}{f_{1/2}} \right)^2 \right]$$

$$f_{1/2} = \frac{f_0}{2Q_L}, P_g = \frac{V_{cav}^2}{4 \frac{r}{Q} Q_L} \left[1 + \left(\frac{\Delta f}{f_0 / 2Q_L} \right)^2 \right]$$

$$Q_{opt} = \frac{f_0}{2\Delta f}, P_{g,min} = \frac{V_{cav}^2}{2r/Q} \frac{\Delta f}{f_0}$$



RF source power calculated for Fermilab's 650 MHz $\beta=0.9$ SRF cavity; $V_{cav}=17.5$ MV $r/Q=638$

Amount of RF source power needed to drive the cavity is highly dependent on the expected detuning frequency shift (Δf) specially for low beam current medium energy particle accelerators where the loaded quality factor is in the order of 10^7 - 10^8 .

Multi-Physics of Super-Conducting Cavities: Microphonics Cont.

Electromagnetic Waves

- Solving only for the RF domain
- Applying the proper boundary conditions

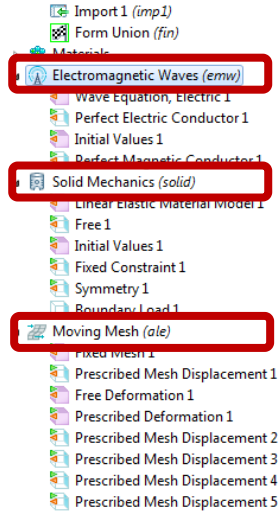
Solid Mechanics

- Solving only for the Cavity Vessel
- Applying the proper fixed constraints, symmetries, displacements, and boundary load

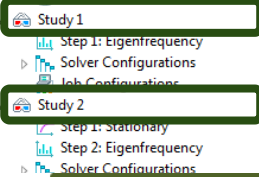
Moving Mesh

- Solving for all domains
- Applying the proper prescribed and free mesh deformation/displacement

Three Multiphysics Modules



Two Simulation Studies



Study₁

- Eigen-frequency (to find f_0)

Study₂

- Stationary (solving only for solid mechanics and moving mesh)
- Eigen-frequency (to find f_p)

EM

- Eigen frequency simulation to find the resonant frequency (f_0)

Solid Mechanics

- Find the deformation under given pressure load (P_L)

Moving Mesh

- Update the mesh after deformation

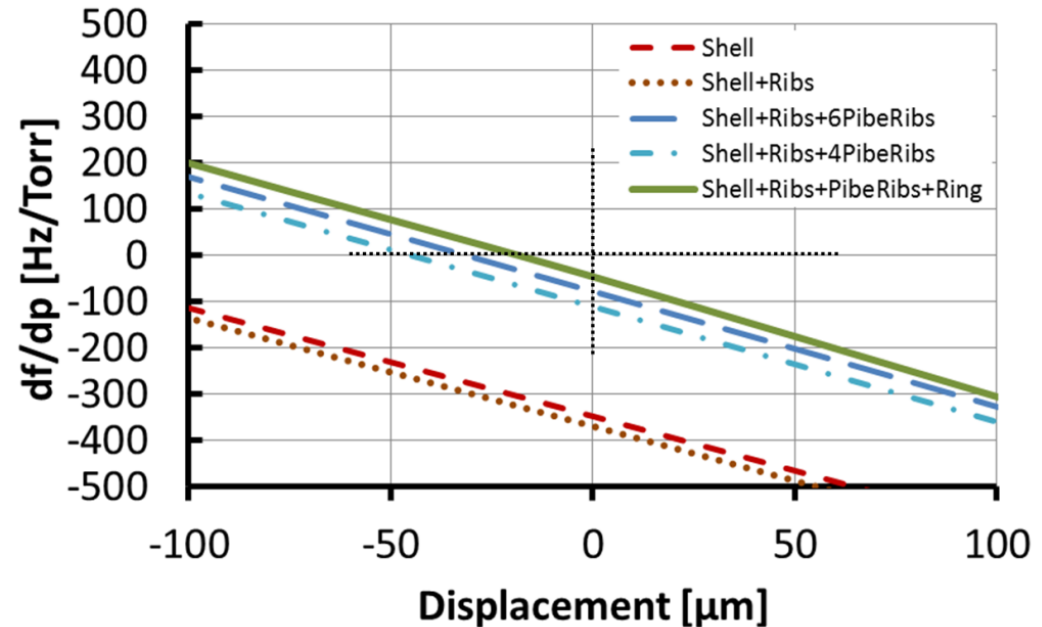
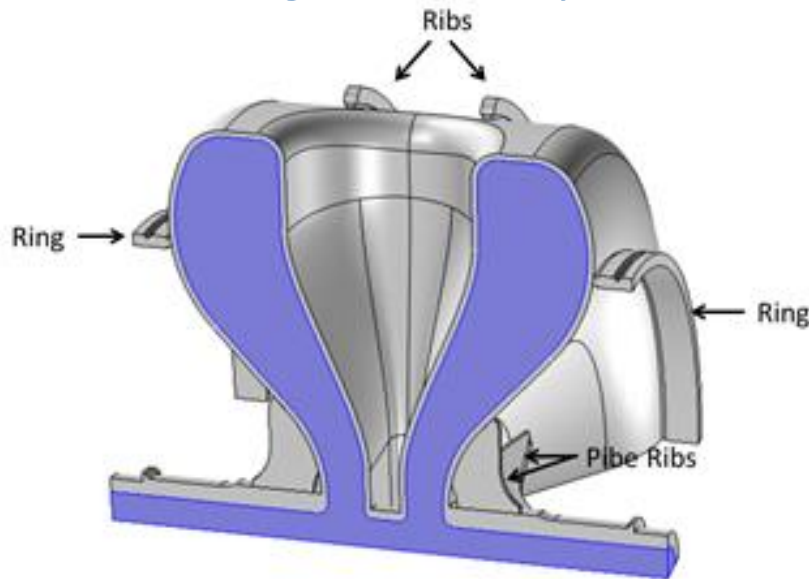
EM

- Eigen frequency simulation to find the resonant frequency after deformation (f_p)

$$\frac{df}{dp} = \frac{f_p - f_0}{P_L}$$

Multi-Physics of Super-Conducting Cavities: Microphonics Cont.

Stiffening the Cavity



- » Pipe Ribs are very important to reduce df/dp
- » Ring between the shell and the Helium vessel would simplify the vessel design

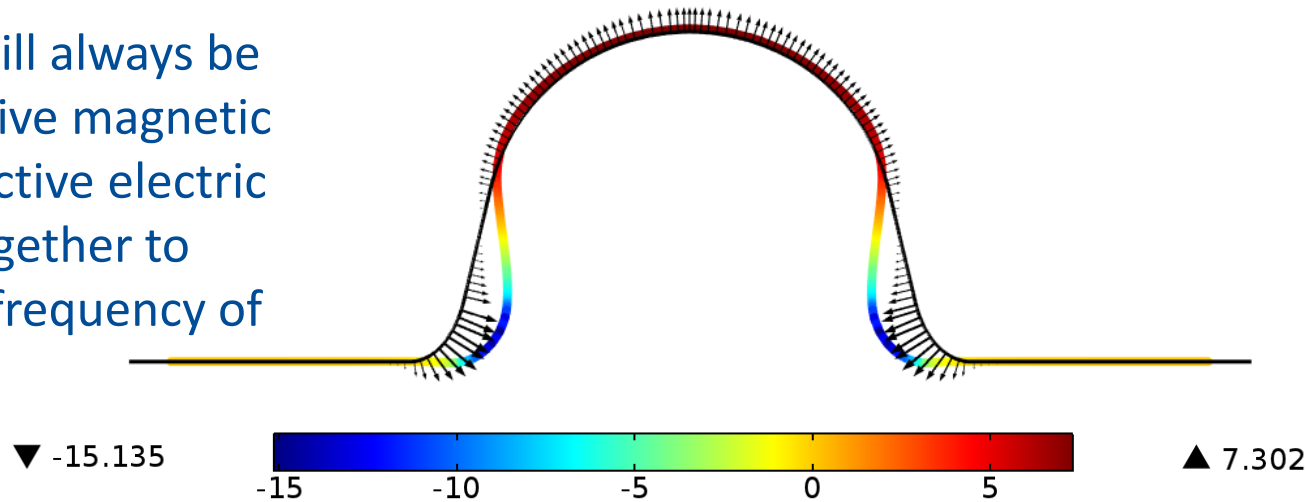
Detuning Simulation: LFD

Electromagnetic fields inside the cavity exerts radiation pressure on the cavity inside walls that is defined as

$$P_{rad} = \frac{1}{4} \left(\mu |H|^2 - \varepsilon |E|^2 \right)$$

Radiation pressure exerted by the magnetic field is positive pushing pressure, while it is negative pulling for the electric field

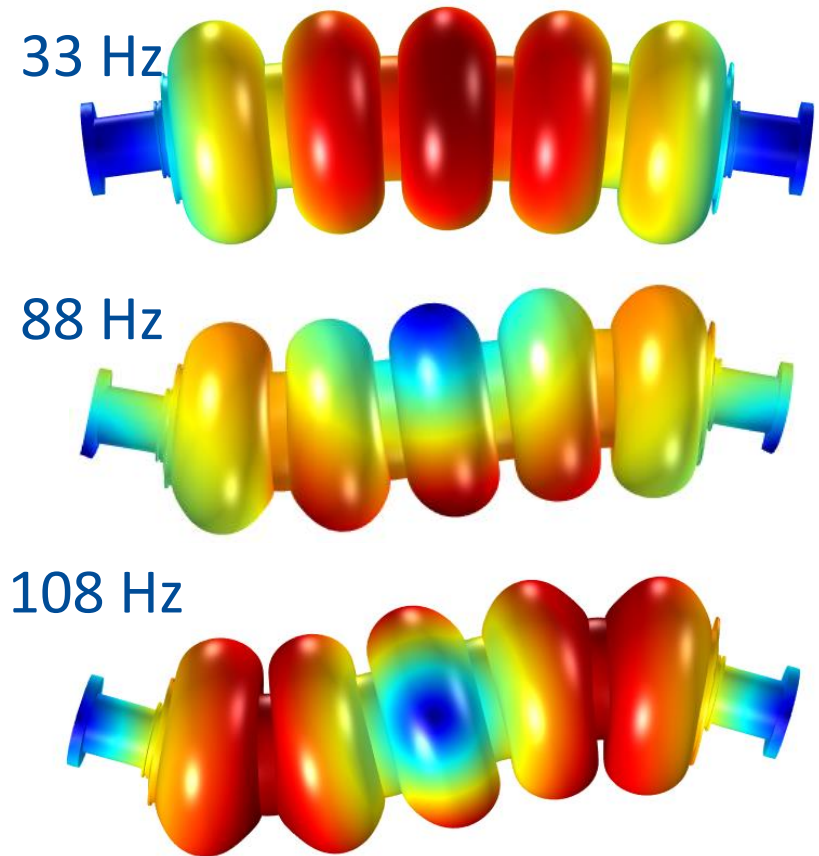
Overall frequency shift will always be negative since the repulsive magnetic field forces and the attractive electric field forces both work together to decrease the resonance frequency of the deformed cavity



Lorentz forces exerted on the 650 MHz $\beta=0.9$ single cell cavity ahead with the radiation pressure values in mbar at the 3.5 MV cavity voltage. Deformation is exaggerated by 20000 times

Detuning Simulation: Mechanical Vibration

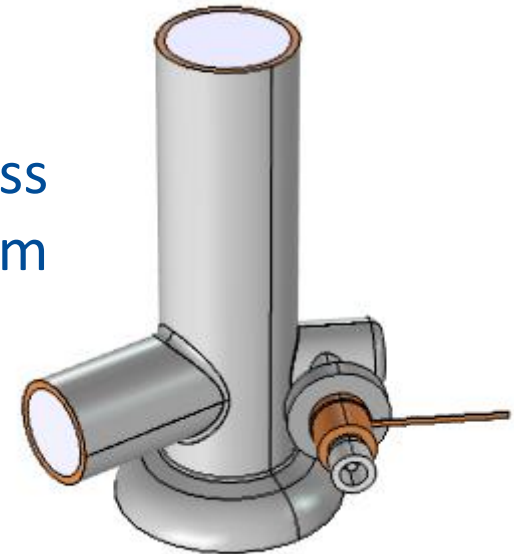
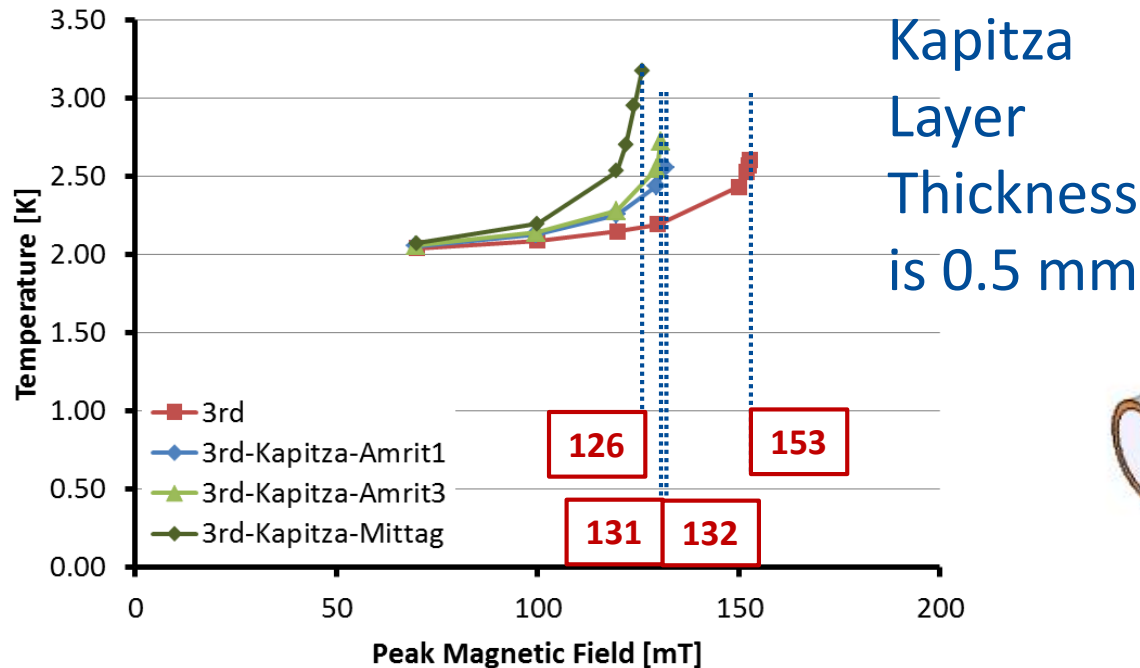
- Modal eigen-frequencies of each cavity structure can be numerically calculated using a solid mechanics solver
- Any modification on the cavity structure would necessarily change the modal frequencies.
- The frequency shift in the electromagnetic resonance frequency due to the excitation of a certain modal eigen-frequency could be computed knowing the energy of that eigen-frequency.
- Moreover, we believe that the modal frequency will be affected by the liquid Helium filling the cavity during operation



Modal frequencies of the
650 MHz $\beta=0.9$ cavity

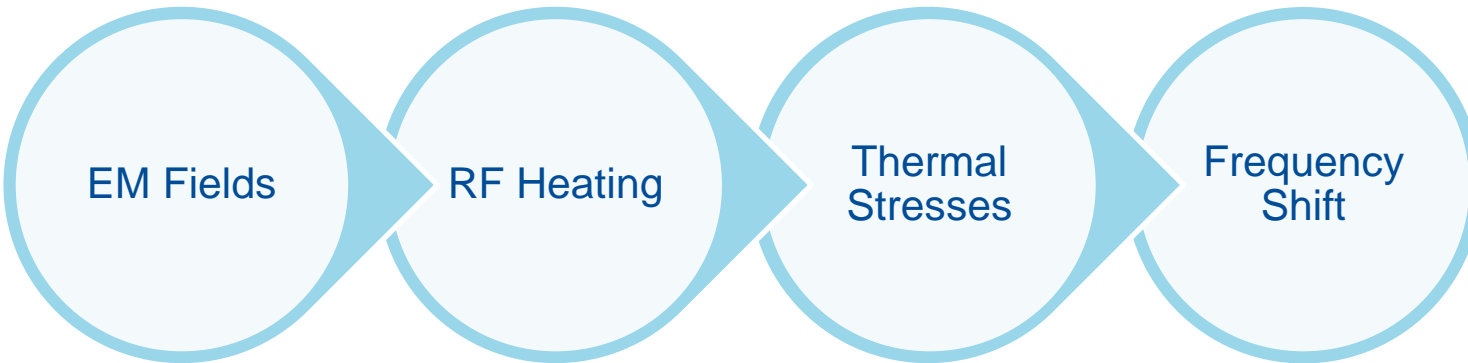
Quench Analysis of Superconducting Cavity

- Given the several models of Kapitza Resistance, we tried to use our experience with the third harmonic cavity to check which one is closer to measurements
- Mittag model looks the closest with quench field 126mT vs 120mT observed in measurements, thus it will be adopted



Multiphysics of Normal Conducting Cavities

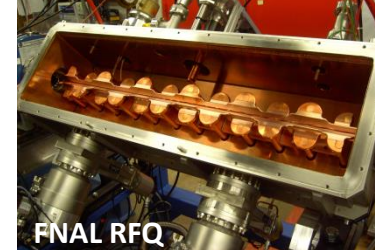
- Copper cavities are being used in many particle accelerators
- RF heating needs to be carefully modeled in such cavities
- Thermal stresses and frequency shifts are main concerns



FNAL Tevatron LINAC Cavities



FNAL Tevatron LINAC Cavities



FNAL RFQ



FNAL Booster Cavity

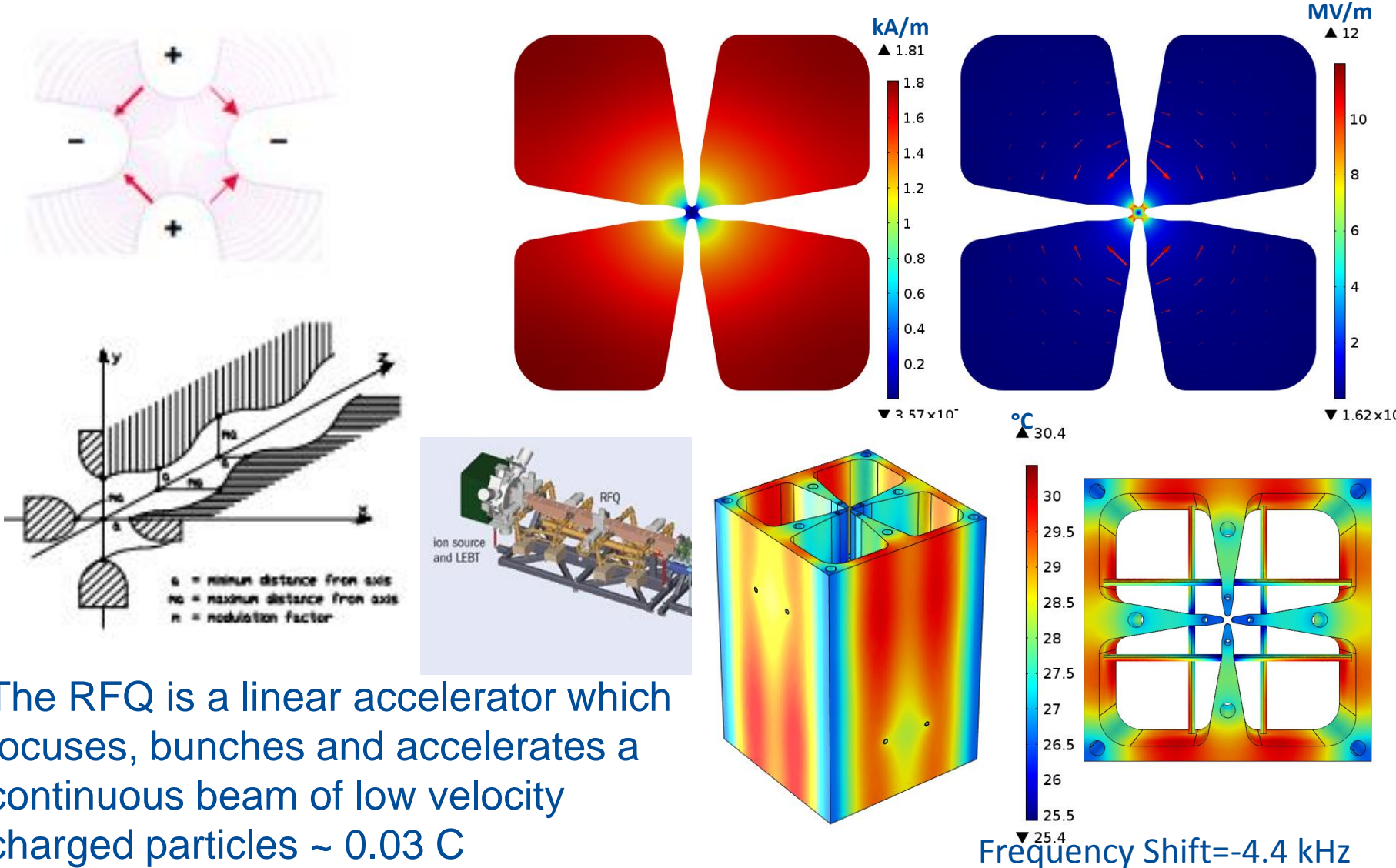
Four Multiphysics Modules

Simulation Studies

- RFQ-EigenModeHeating_PISL_Period_FinerA
 - Global Definitions
 - Model 1 (mod1)
 - Definitions
 - Geometry 1
 - Materials
 - Electromagnetic Waves (emw)
 - Heat Transfer (ht)
 - Solid Mechanics (solid)
 - Moving Mesh (msh)
 - Mesh 1
 - Study 1
 - Step 1: Eigenfrequency
 - Step 2: Stationary
 - Step 3: Stationary 2
 - Step 4: Eigenfrequency 2
 - Solver Configurations
 - Results
 - Data Sets



Multi-Physics Analysis of Radio Frequency Quadrupole

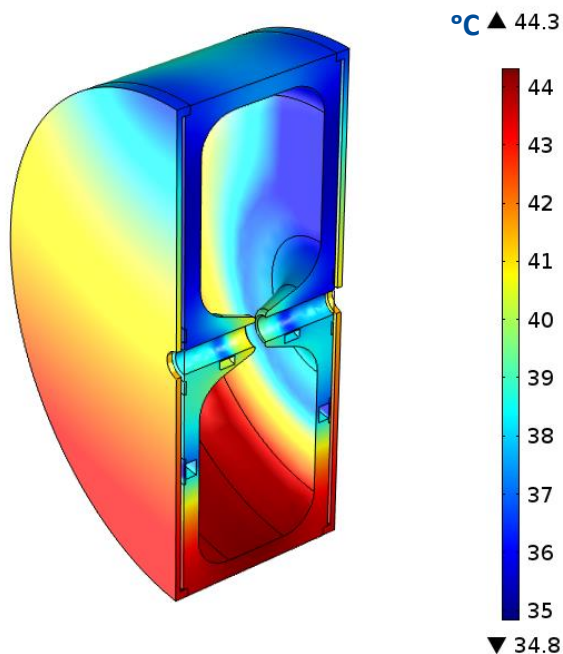


The RFQ is a linear accelerator which focuses, bunches and accelerates a continuous beam of low velocity charged particles $\sim 0.03 C$

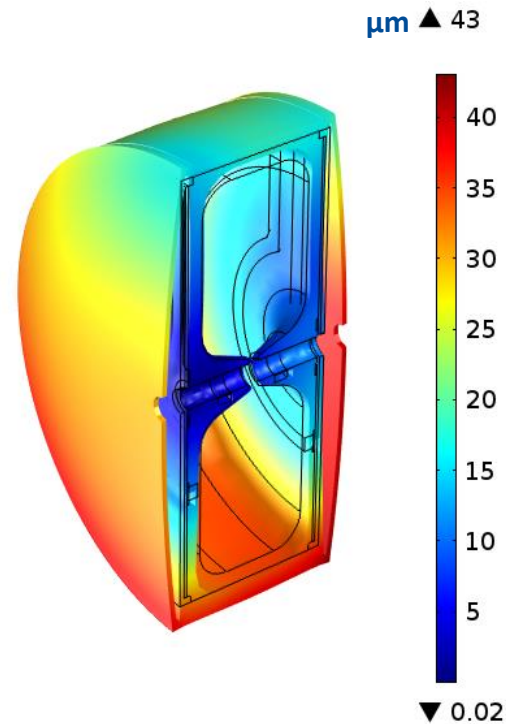
Multiphysics of a Buncher Normal Conducting Cavity

- Input Port Power is 3725 Watt, adjusted to induce 127 KV (75 KV Effective)
- Fixed Beam Pipe in transverse plane

Temperature Profile



Thermal Displacement

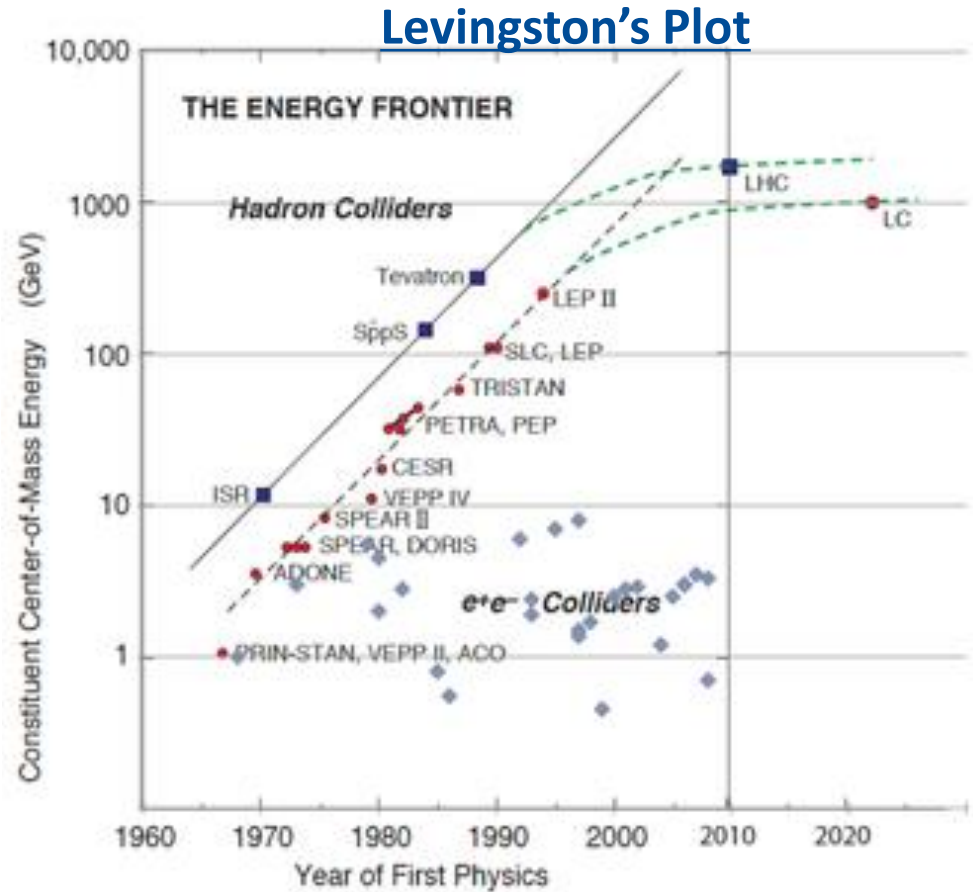


Amount of frequency shift due to the thermal stresses is -28.7 KHz

Future of Particle Accelerators

- » Today more than 30,000 accelerators are in operation around the world—in industry, in hospitals, and at research institutions
- » Many large scale projects are on going or coming soon!

Project	SRF Cavities	Cryo Modules	Est. Market (in millions)
Continuous Electron Beam Accelerator Facility (CEBAF) Upgrade, Thomas Jefferson Lab National Accelerator Facility, Newport News, VA	86	10	17
Facility for Rare Isotope Beams (FRIB), Michigan State University, East Lansing, MI	336	45	100
Proposed Project X, Fermilab, Batavia, IL	445	58	87
Proposed Cornell Energy Recovery LINAC, Cornell University, Ithaca, NY	304	58	57
Proposed SNS Upgrade, Oak Ridge National Laboratory (ORNL), Oak Ridge, TN	36	9	18
TOTAL	1207	160	279

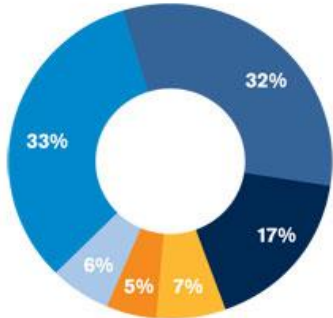


Livingston: the energy records achieved by new machines by a factor of 10 every six years

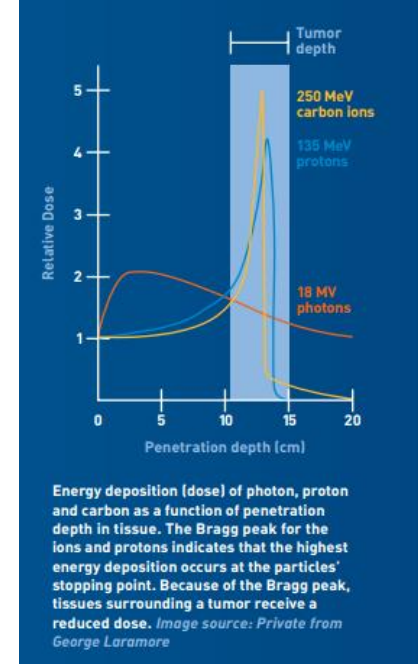
Future of Particle Accelerators Cont.

Markets for industrial electron beams total \$50 billion per year.

Image source: IAEA Working Material on Industrial Electron Beam Processing



- Wire cable tubing
- Ink curing
- Shrink film
- Service
- Tires



	Low energy	Medium energy	High energy
Energy range	70 keV–300 keV	300 keV–5 MeV	5 MeV–10 MeV
Features	Wide unscanned beams less ≤ 3 m	Scanned beams ≤ 3 m	Linacs or SRF
Current applications	<ul style="list-style-type: none"> • Curing of inks • Crosslinking of polymers • Surface sterilization • Remediation of liquids and gases 	<ul style="list-style-type: none"> • Crosslinking of wire and cable insulation • Crosslink heat-shrinkable plastic tubing • Manufacture of closed-cell foam • Crosslink plastic • Crosslink rubber • Medical sterilization 	<ul style="list-style-type: none"> • Bulk sterilization of medical devices • Crosslinking thicker plastics



Concept for a compact proton therapy system for treating cancer patients, based on a dielectric wall accelerator Image courtesy of S. Hawkins, Lawrence Livermore National Laboratory

Summary

- » A particle accelerator is a device that uses electromagnetic fields to propel charged particles to high speeds
- » It consists of a series of cryomodules. Each cryomodule houses several RF cavities and magnets
- » Normal conducting and superconducting cavities are used in particle accelerators
- » SRF cavities needs a series of complicated multiphysics analyses to properly address the design issues (microphonics and Lorentz force detuning)
- » Normal conducting cavities needs also a series of complicated multiphysics analyses (electromagnetic heating is the main concern)

Thanks for your Attention

