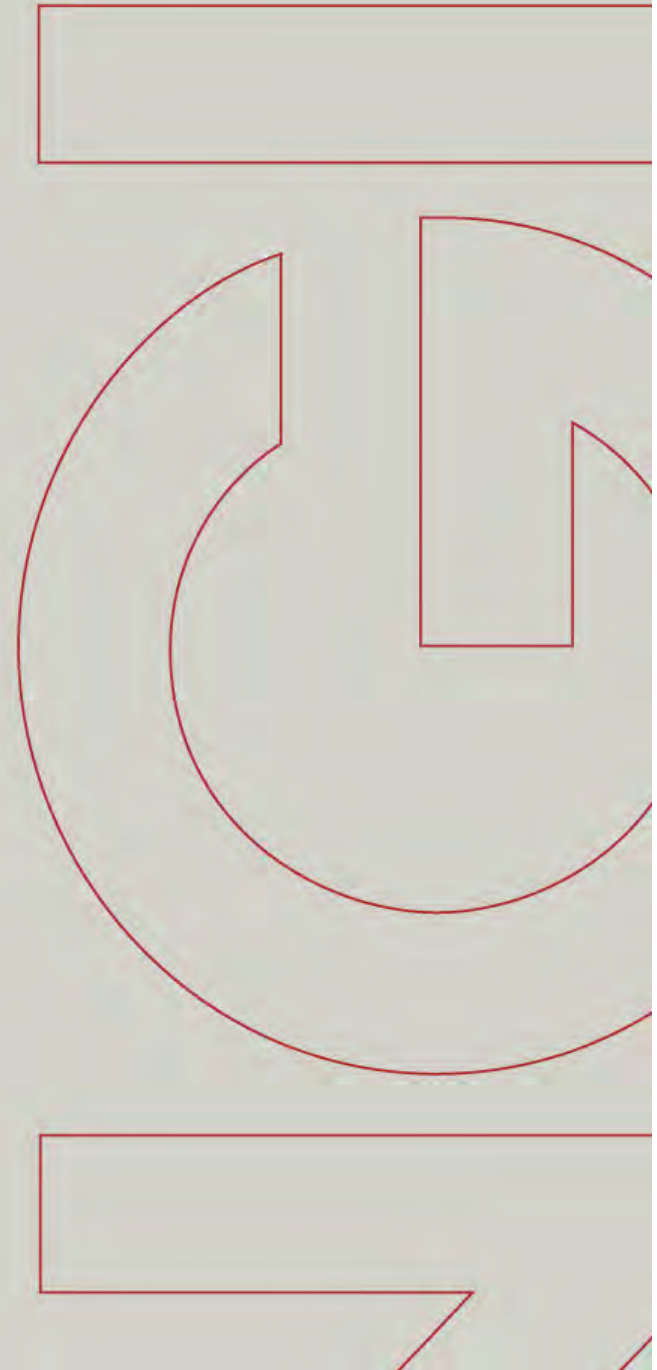


# Absorbing boundary domain for CSEM 3D modelling

COMSOL User Conference, Nov. 2010, Paris

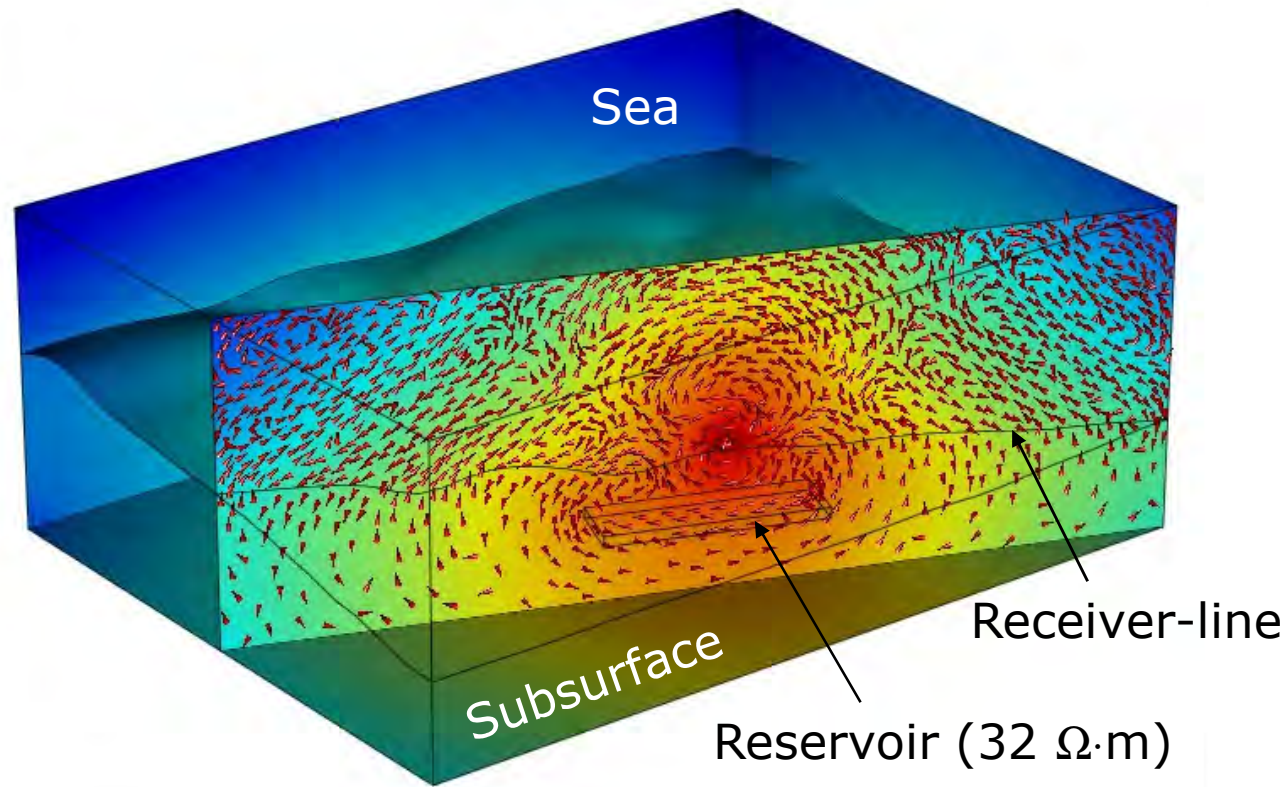
J. Park, T.I. Bjørnarå (NGI, Oslo, Norway),  
B.A. Farrelly (MultiField Geophysics AS,  
Bergen, Norway)



# Content

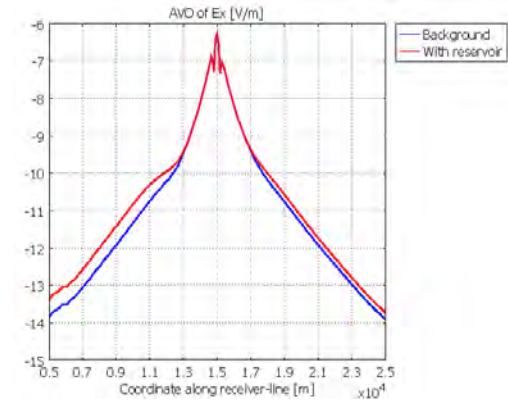
- Marine CSEM, principle
- PML, (short) history
- Proposed PML/ABD and implementation to COMSOL Multiphysics, RF module
- Test examples:
  1. Deep water
  2. Shallow water
- Comments on mesh
- Summary

# Marine CSEM, principle

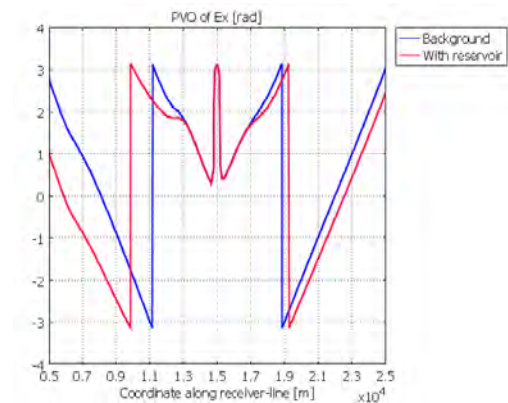


Source: HED, 0.25 Hz. Plot: Electric field

### AVO, receiver-line



### PVO, receiver-line



INGI

## PML, history

**Complex-value stretching**  
**For our application: Not efficient**  
**enough due to high attenuation**

- Berenger, J., A perfectly matched layer for the absorption of electromagnetic waves, J. Comput. Phys. 114(2), 185-200. (1994).
- Etc.

Yet,

**Real-value stretching**

- Lysmer, J., M. Tabatabaie-Raissi, F. Tajirian., S. Vahdani,. and F. Ostadan (1981). SASSI - A system for analysis of soil-structure interaction, Report UCB/GT 81-02, Univ. of California, Berkeley, USA.

NING

comsol\_2010\_model\_10\_QE.mph - COMSOL Multiphysics

File Edit Options Help

Selection List Settings

**Analytic**

Function Name

Function name: Spml

Parameters

Expression:  $x\_local * a^{(abs(x\_local/h0))}$

Arguments:  $x\_local, a, h0$

Derivatives: Automatic

Periodic Extension

Advanced

Plot Parameters

Model Builder

comsol\_2010\_model\_10\_QE.mph (root)

- Global Definitions
  - Parameters
  - Analytic 1 (Spml)
- Model 1 (mod1)
  - Definitions
  - Geometry 1
  - Materials
  - Electromagnetic Waves (rfw)
  - Meshes
- Study 1
- Results

Material Browser Model Library Progress Messages Graphics

Real-value, exponential stretching:

$$\xi = x_0 a^{x_0/h_0} \geq 10d$$

$\xi$  Stretched coord.

$x_0$  Unstretched coord. [3-10km]\*

$a$  Parameter, [1, $\pi$ ], eg.  $\pi/2^*$

$h_0$  Parameter; element size in computational domain

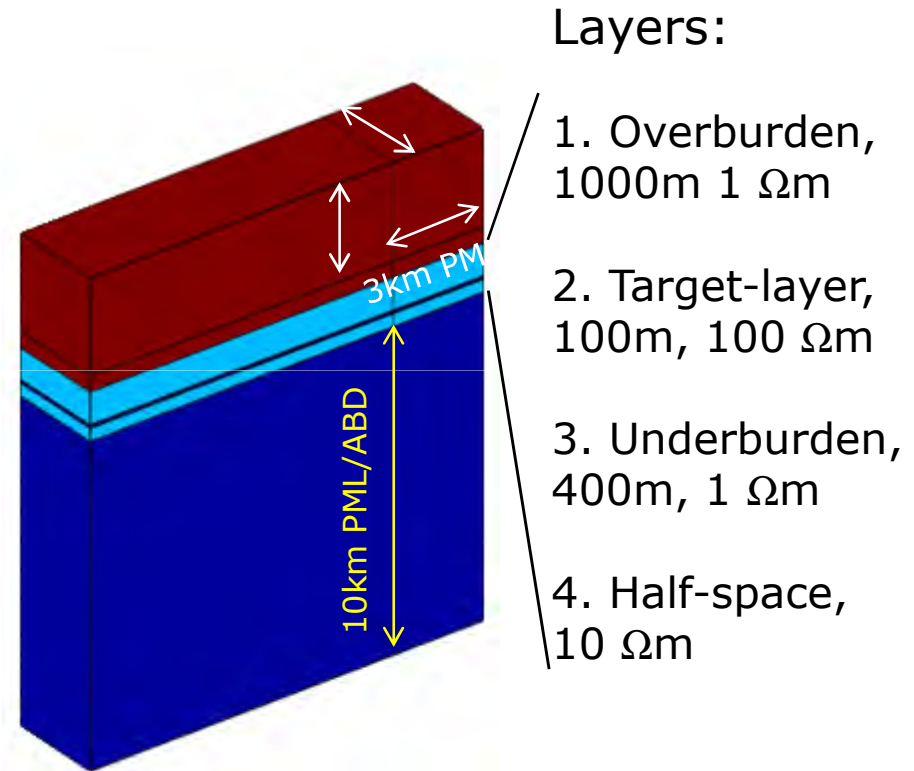
$d$  Skin depth

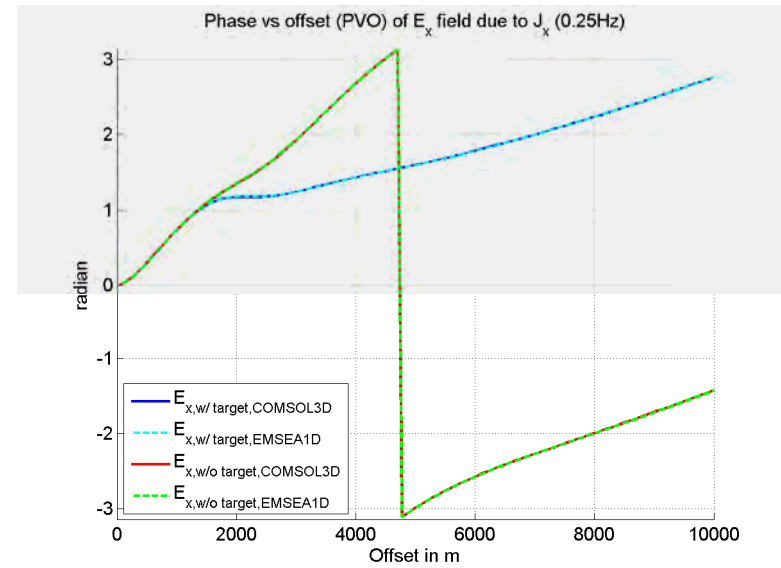
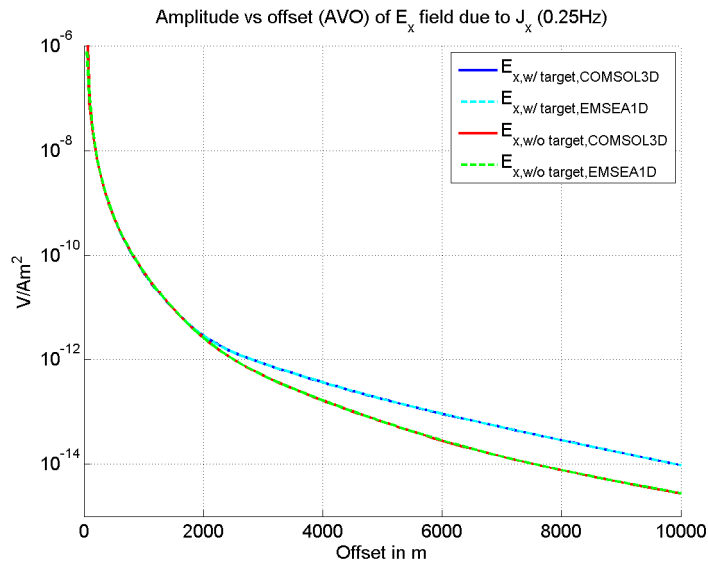
(\* empirical)

Working set: 266 MB Virtual memory: 272 MB

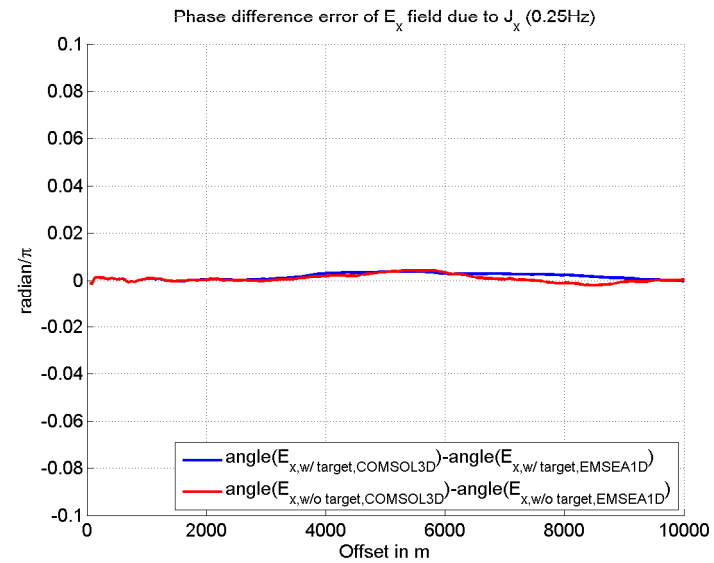
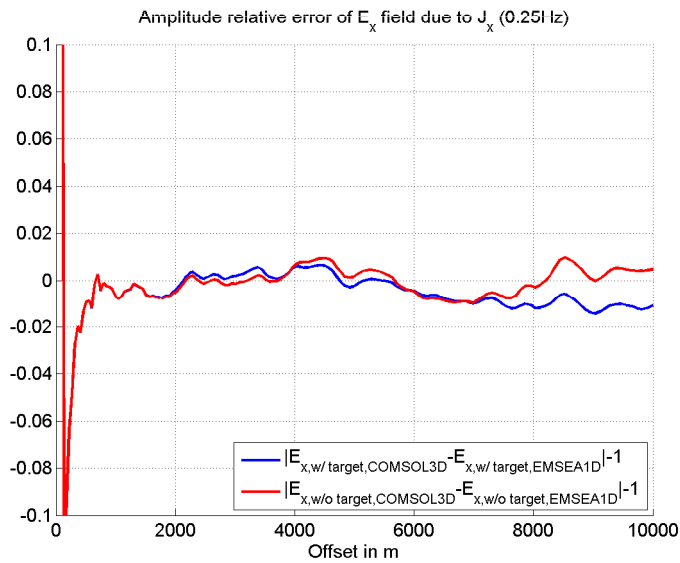
# Test example 1: infinite-deep water without air-wave effect

- Infinite deep seawater
- 0.25Hz inline HED
- Receiver line: 0–10km, or 0–5km on seabed
- The subsurface consists of four layers
- ABD sizes are 3 and 10 km

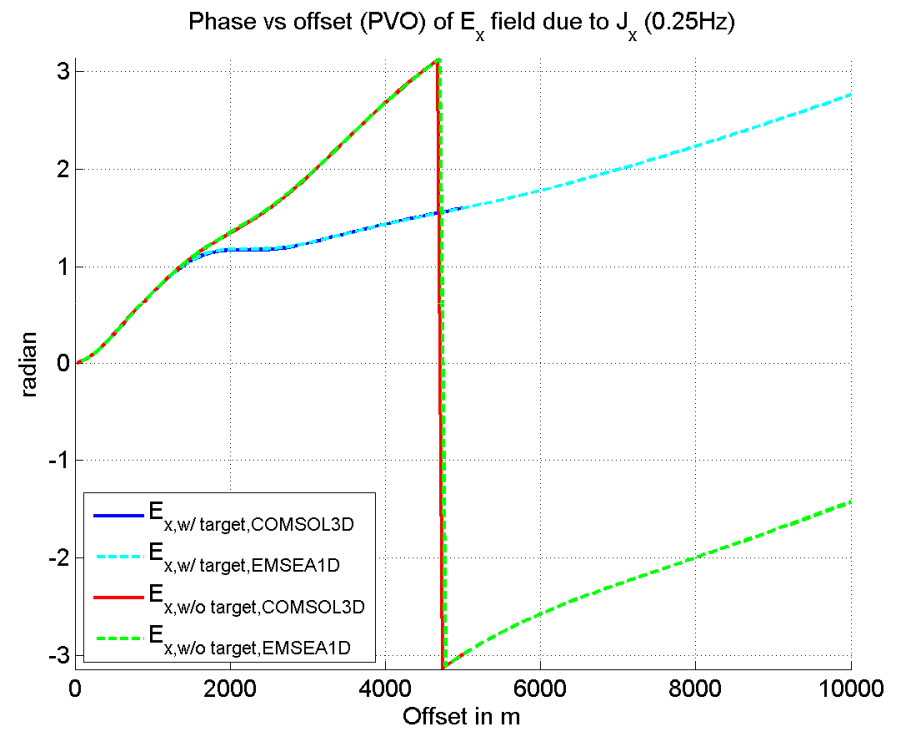
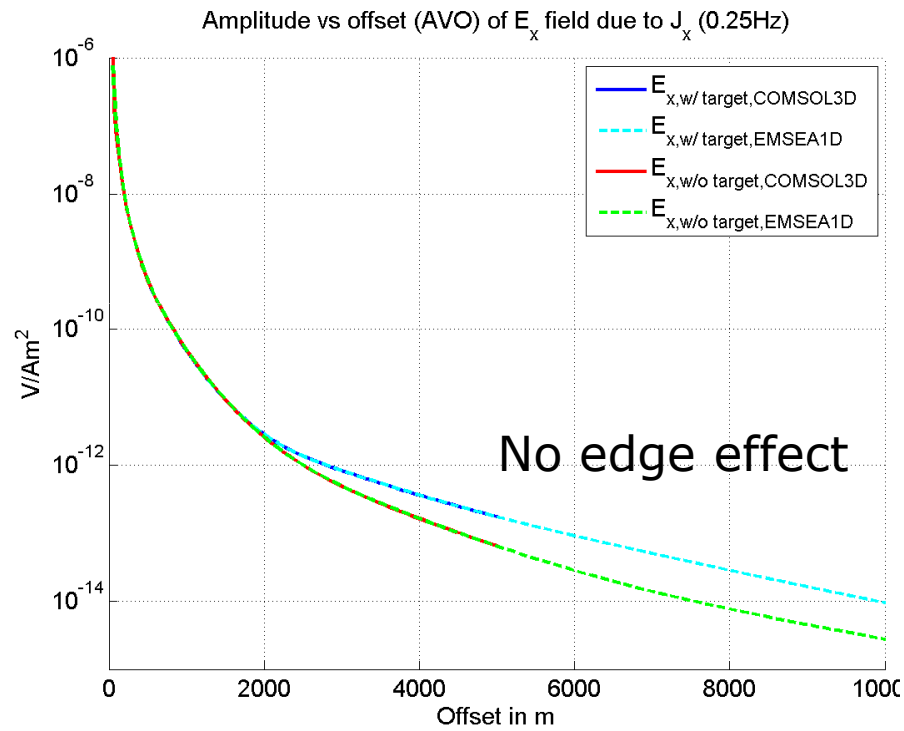




## (n)AVO and (d)PVO for 10km model



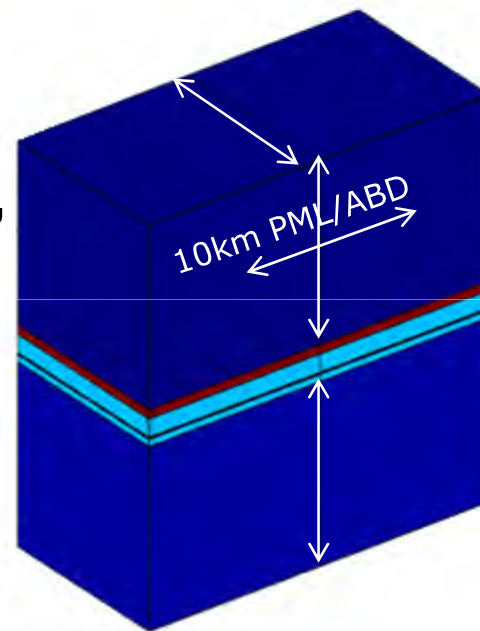
# AVO and PVO for 5km model





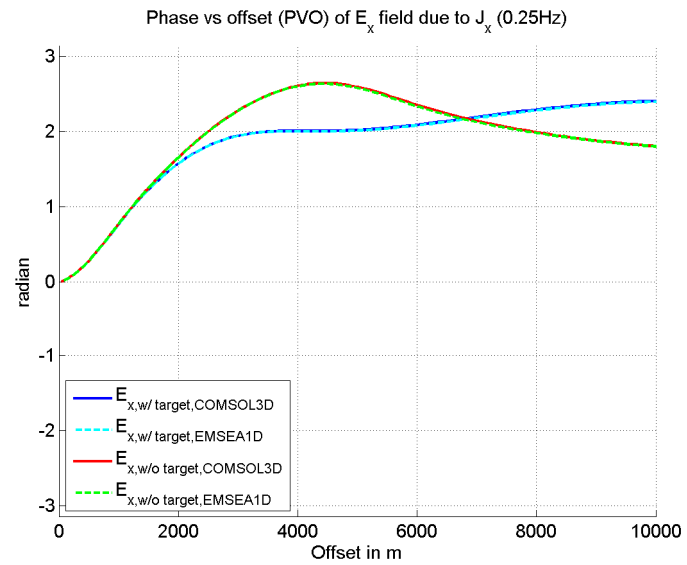
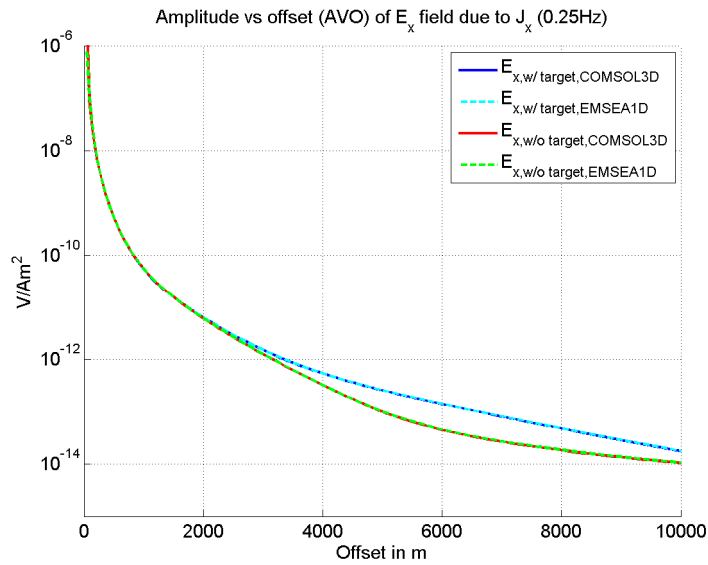
## Test example 2: shallow water with air-wave effect

- 500m water depth
- 0.25Hz inline HED
- Receiver line: 0–10km, or 0–5km on seabed
- Subsurface consists of four layers
- ABD size is 10km

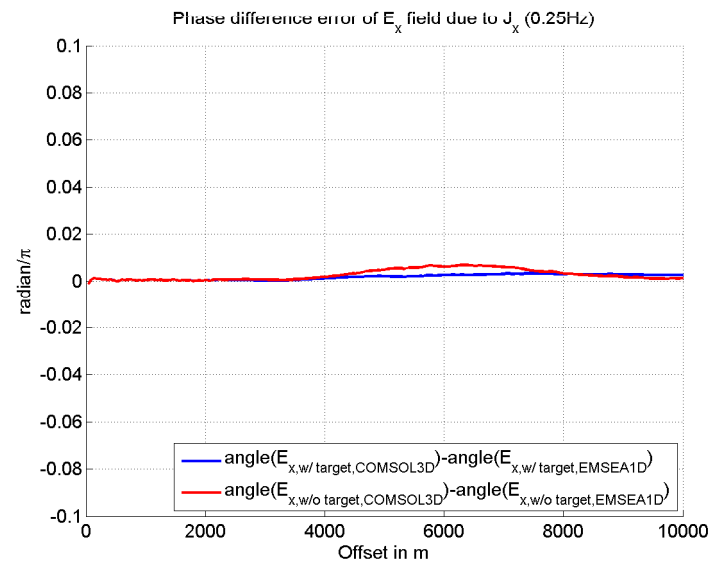
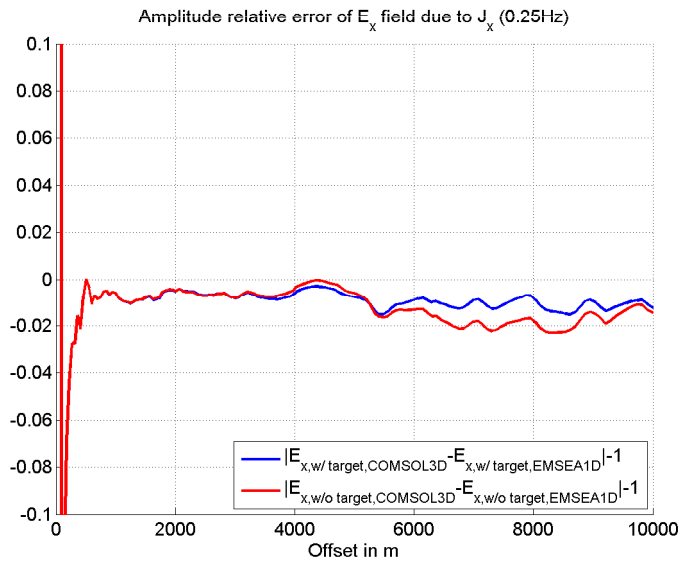


### Layers:

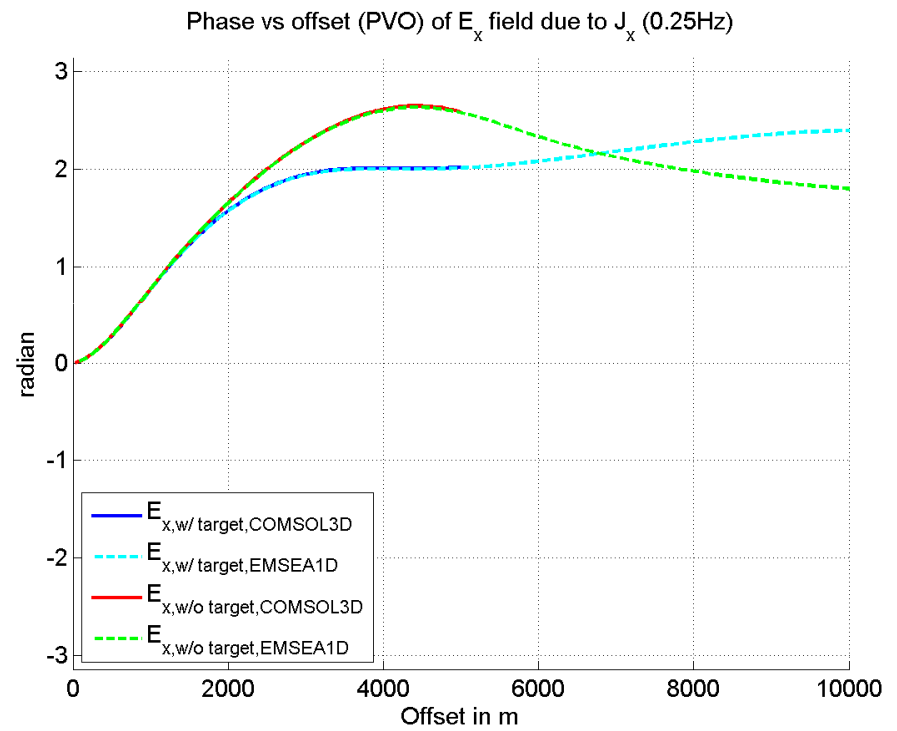
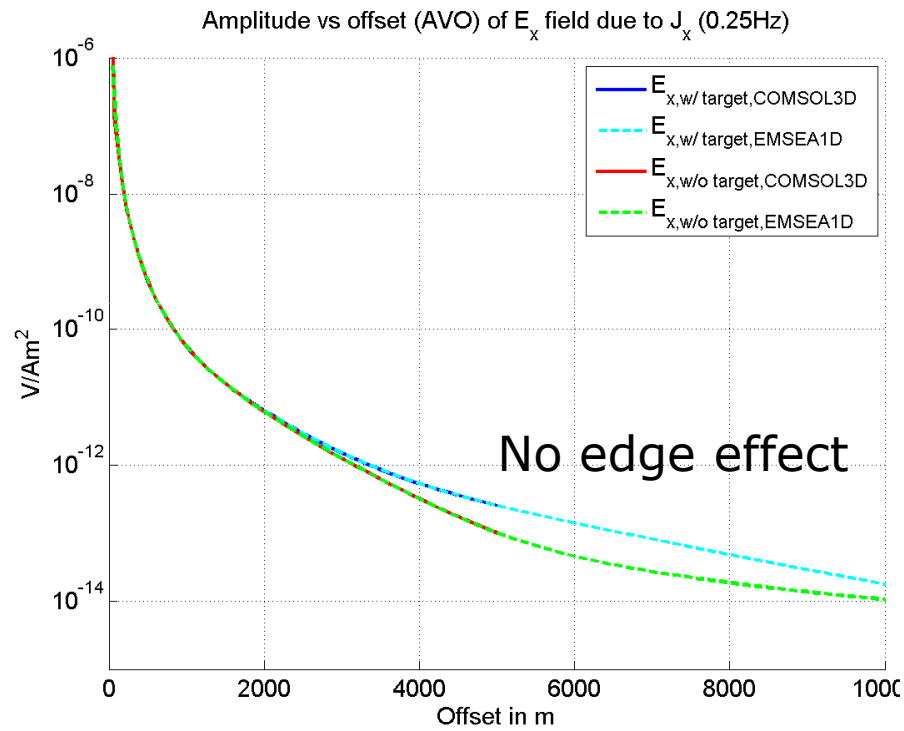
1. Overburden, 1000m, 1  $\Omega$ m
2. Target-layer, 100m, 100  $\Omega$ m
3. Underburden, 400m, 1  $\Omega$ m
4. Half-space, 10  $\Omega$ m



## (n)AVO and (d)PVO for 10km model

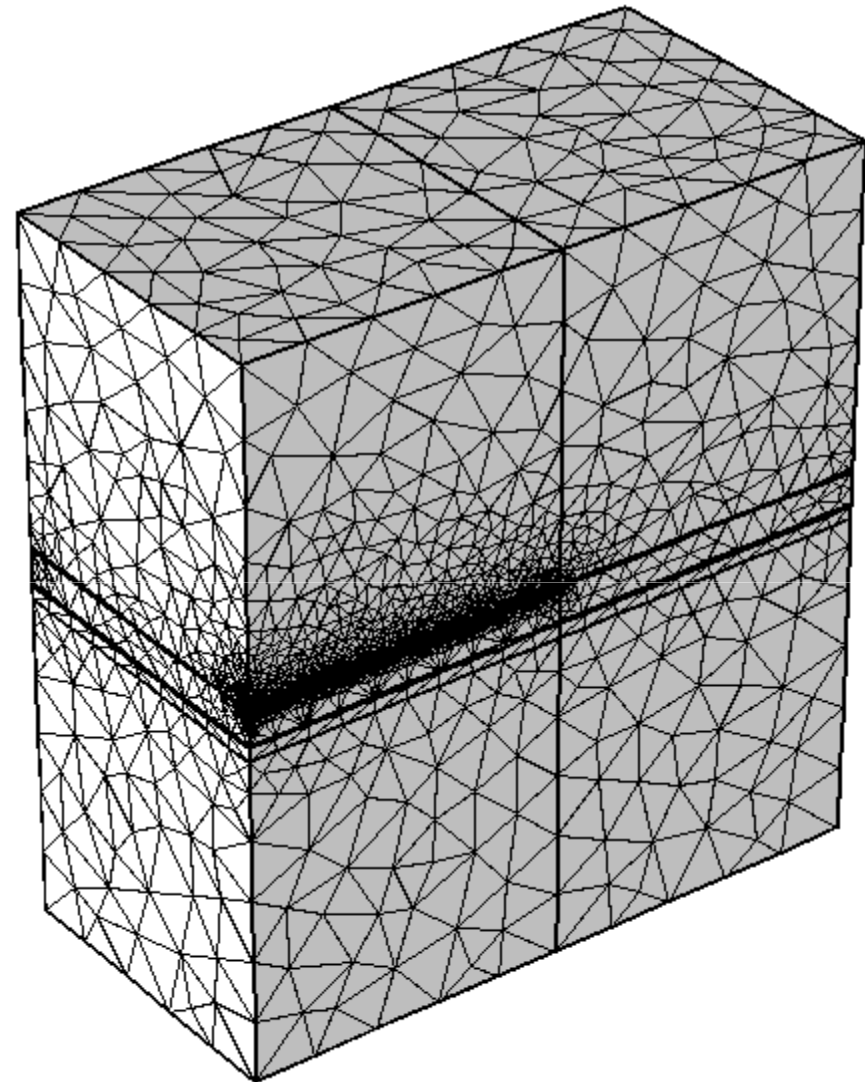


# AVO and PVO for 5km model



# Mesh

- Note that mesh size in ABD is rather big
- Note that dense mesh near the the receiver lines are made



# Summary

- An efficient absorbing boundary domain technique is implemented and evaluated in COMSOL
  - Real-valued (and complex-valued) exponential stretching
  
- Acknowledgements:
  - Thank to Statoil, MultiField Geophysics, and NGI for their financial support for this study and permission to present